

WSRL-0039-TR



DEPARTMENT OF DEFENCE

DEFENCE SCIENCE AND TECHNOLOGY ORGANISATION
WEAPONS SYSTEMS RESEARCH LABORATORY

DEFENCE RESEARCH CENTRE SALISBURY
SOUTH AUSTRALIA

TECHNICAL REPORT

WSRL-0039-TR

THE ANALYSIS OF TRAJECTORY AND SOLAR ASPECT ANGLE RECORDS
OF SHELL FLIGHTS. THEORY AND COMPUTER PROGRAMS.

R.L. POPE

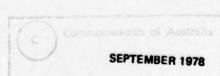


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(1) Sep 78

DEPARTMENT OF DEFENCE

AR-001-389

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SUMMARY

The theory and computer programs described in this report form part of a research programme in nonlinear dynamics. Methods and computer programs for obtaining aerodynamic coefficients from free flight trials of shells have been The data from the trials consists of both trajectory data from either radar tracking of the shell or ballistic camera records of a flashing light carried in the shell, and complementary solar aspect angle measurements from The data analysis techniques will be used to yawsondes. investigate the exterior ballistics of shells. As well as a tool for investigating dynamic stability problems concerning standard or modified shells they offer a new and more efficient approach to developing a Fire Control Model. An interesting facet of the data analysis is the representation of the aerodynamic force coefficients as analytic functions of Mach number, an approach which has potential for greater accuracy than the piecewise linear representation which is in general use. facilitate use of the programs by the reader, program listings are supplemented by tables of input variables and sample output. Results from test runs using artificially generated data are discussed.

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URAGIFIED 9 26 062

Security classification of this page UNCLA	ASSIFIED
DOCUMENT NUMBERS	2 SECURITY CLASSIFICATION
AR AR-001-389 Number:	a. Complete UNCLASSIFIED Document:
Report Number: WSRL-0039-TR	b. Title in Isolation: UNCLASSIFIED
Other Numbers:	c. Summary in Isolation: UNCLASSIFIED
	RY AND SOLAR ASPECT ANGLE RECORDS FROM AND COMPUTER PROGRAMS.
4 PERSONAL AUTHOR(S):	5 DOCUMENT DATE: September 1978
R.L. Pope	6 6.1 TOTAL NUMBER OF PAGES 81
	6.2 NUMBER OF REFERENCES: 18
7 7.1 CORPORATE AUTHOR(S):	8 REFERENCE NUMBERS
Weapons Systems Research Laboratory	a. Task: DST 76/011 b. Sponsoring DST 76/011
7.2 DOCUMENT SERIES AND NUMBER Weapons Systems Research Laboratory 0039-TR	9 COST CODE: 331251
10 IMPRINT (Publishing organisation)	11 COMPUTER PROGRAM(S)
Defence Research Centre Salisbury	(Title(s) and language(s))
LA DELEGATION AND AND AND AND AND AND AND AND AND AN	
12 RELEASE LIMITATIONS (of the document): Approved for Public Release	

UNCLASSIFIED

13 ANNOUNCEMENT LIMITATIONS (of the information on these pages):

No limitation.

Computer programs Trajectories DESCRIPTORS: Projectiles a. EJC Thesaurus Projectile trajectories Terms Yaw Ballistics Ballistic trajectories Solar aspect b. Non-Thesaurus Shells angle Terms Yawsondes Parameter estimation Free flight data analysis

15 COSATI CODES: 1904 2011

16 LIBRARY LOCATION CODES (for libraries listed in the distribution):

SW SR SD AACA

7 SUMMARY OR ABSTRACT:

(if this is security classified, the announcement of this report will be similarly classified)

The theory and computer programs described in this report form part of a research programme in nonlinear dynamics. Methods and computer programs for obtaining aerodynamic coefficients from free flight trials of shells have been developed. The data from the trials consists of both trajectory data from either radar tracking of the shell or ballistic camera records of a flashing light carried in the shell, and complementary solar aspect angle measurements from yawsondes. The data analysis techniques will be used to investigate the exterior ballistics of shells. As well as a tool for investigating dynamic stability problems concerning standard or modified shells they offer a new and more efficient approach to developing a Fire Control Model. An interesting facet of the data analysis is the representation of the aerodynamic force coefficients as analytic functions of Mach number, an approach which has potential for greater accuracy than the piecewise linear representation which is in To facilitate use of the programs by the reader, program listings are supplemented by tables of input variables and sample output. Results from test runs using artificially generated data are discussed.

Security classification of this page:

UNCLASSIFIED

TABLE OF CONTENTS

		Page No).
1.	INTRODUCTION	1 - 2	
2.	ANALYTICAL REPRESENTATION OF THE VARIATION OF AERODYNAMIC		
	COEFFICIENTS WITH MACH NUMBER	2 - 4	
	2.1 Axial force	2 - 3	
	2.2 Normal force derivative	4	
	2.3 Roll damping derivative	4	
3.	TRAJECTORY DATA ANALYSIS	4 - 9	
	3.1 Mathematical model	5 - 7	
	3.2 Program SHELTRAJ	7 - 9	
	3.2.1 Input Accession For	8 - 9	
	3.2.2 Output	9	
4.	YAWSONDE DATA ANALYSIS DDC TAB Unconcurred	9 - 14	1
	4.1 Yawsonde usage Judification	10 - 11	l
	4.2 Mathematical model	12 - 13	3
	4.3 Program YAWSONDE Distribution/	13 - 14	1
	4.3.1 Input	14	
	4.3.2 Output	14	
5.	PROGRAM TESTING Dist special	14 - 17	7
	5.1 Program SHELTRAJ	15 - 16	5
	5.2 Program YAWSONDE	17	
6.	SUMMARY OF RESULTS	17	
7.	APPLICATION OF RESULTS	18 - 19	9
	NOTATION	20 - 23	3
	REFERENCES	24 - 25	5
	LIST OF APPENDICES		
	I NR3634 DRAG CURVE	26 - 27	7
1	I CORIOLIS AND GRAVITY COMPONENTS	28	
11	I PARTIAL DERIVATIVES WITH RESPECT TO PARAMETERS FOR SHELTRAJ	29 - 32	2
I	V LISTING OF PROGRAM SHELTRAJ	33 - 39	9
	V YAWSONDE CALIBRATION	40 - 41	1
v	I LISTING OF PROGRAM YAWCAL	42	
VI		43	
4.1	1 OUDAN NOTECT MODE	70	

		Page	No.
VIII	LISTING OF PROGRAM ASPECT	44 -	45
IX	PARTIAL DERIVATIVES WITH RESPECT TO PARAMETERS FOR YAWSONDE	46 -	47
х	LISTING OF PROGRAM YAWSONDE	48 -	53
	LIST OF TABLES		
1.	TYPICAL AERODYNAMIC DATA FOR A SHELL	54	
2.	FITTING ANALYTIC CURVES TO THE AXIAL FORCE COEFFICIENT		
	(A) NR3634	55	
	(B) GAVRE	55	
3.	ANALYTIC REPRESENTATIONS FOR OTHER COEFFICIENTS		
	(A) NORMAL FORCE DERIVATIVE	55	
	(B) ROLL DAMPING DERIVATIVE	55	
4.	DESCRIPTION OF CARD INPUT TO SHELTRAJ	56 -	57
5.	SAMPLE INPUT DECK FOR SHELTRAJ		
	(A) FORCES	58	
	(B) ROLLING MOMENTS	59	
6.	SIMULATED EXPERIMENTAL DATA FOR SHELTRAJ	60 -	61
7.	BEGINNING AND END OF OUTPUT FROM SAMPLE INPUT FOR SHELTRAJ		
	(A) FORCES	62 -	63
	(B) ROLLING MOMENTS	64 -	65
8.	DESCRIPTION OF CARD INPUT TO YAWCAL	66	
9.	DESCRIPTION OF CARD INPUT TO ASPECT	67	
10.	DESCRIPTION OF CARD INPUT TO YAWSONDE	68 -	69
11.	SAMPLE INPUT DECK FOR YAWSONDE	70	
12.	SIMULATED EXPERIMENTAL DATA FOR YAWSONDE		
	(A) TRAJECTORY MEASUREMENTS	71	
	(B) YAWSONDE MEASUREMENTS	72	
13.	BEGINNING AND END OF OUTPUT FROM SAMPLE INPUT TO YAWSONDE	73 -	75

LIST OF FIGURES

- 1. Residues for fitted axial force curves
- 2. Residues for fitted normal force derivative curves
- 3. Residues for fitted roll damping derivative curves
- 4. Schematic representation of a yawsonde
- 5. Typical yawsonde calibration curve
- 6. Variation of complementary solar aspect angle with shell elevation
 - (a) heading 300 degrees T
 - (b) heading due north
- 7. Conditions for detecting the sun
- 8. Comparison of methods for estimating aerodynamic force coefficients
 - (a) axial force
 - (b) normal force derivative
- 9. Effects of noise on estimation of roll damping moments

1. INTRODUCTION

In recent years the development of new flight instrumentation for shells and new sophisticated methods of analysing free flight data has resulted in a substantial increase in the possible applications of artillery shell flight trials. The developments which have resulted in important gains in the study of the flight behaviour of shells include the invention of the solar aspect angle sensor or yawsonde(ref.1) and the many improvements to it, some of which are described in reference 2. Other developments of note include the modified point mass or four degree of freedom shell trajectory model(ref.3), and the application of parameter estimation methods to the analysis of free flight data (ref.4,5,6).

One potential application of parameter estimation techniques is in the preparation of a Fire Control Model for a shell(ref.7). Currently, the model is made as accurate as possible using wind tunnel data, then modifications to produce a final version of the model are made, using scaling factors obtained by calibrating the four degree of freedom model against impact point data from test firings. The method is costly because the number of firings is very large and the calibration complex. By using parameter estimation techniques to analyse trajectory data derived from radar or other projectile tracking systems such as the flashing light methods described in reference 8, it is possible to substantially reduce the cost of developing a Fire Control Model.

Another major area of application for the yawsonde and associated parameter estimation algorithms is investigation of shell stability. There are many occasions in the development and testing of shells when there is a requirement for free flight investigation of dynamic stability. Such a requirement may result from changes to the external appearance of the shell to meet the need for a long range, low drag shell or from the need for terminal guidance by canard control. In addition, there are often unexpected problems with shells which cannot be explained without using yawsondes to gather further information on the free flight behaviour of such "rogue" shells.

The U.K. is currently developing a method which uses radar tracking data to produce the Fire Control Model from which aiming tables for shells are constructed(ref.7). The USA has been using yawsonde and radar data for some time now to study dynamic stability and anomalous flight behaviour of shells. The potential savings of these techniques in all areas of research, development and usage of artillery shells are so large that Defence Research Centre Salisbury has begun a program which will lead to the development of these skills. Such skills can then be applied with substantial benefits in many areas.

The present report describes the analysis methods and computer programs which will be used to process the data from the preliminary trials. The parameter estimation algorithm used presently is a simple minimum variance application (ref.4,5). This could be improved considerably by using maximum likelihood estimators(ref.7) and Bayesian methods. However, the minimum variance estimator should work satisfactorily in preliminary trials. The first major use of these programs will be a study to quantify the advantages of using parameter identification techniques to construct a Fire Control Model from trajectory measurements. Such an assessment will also involve estimating the accuracy of various alternative tracking techniques and the effect of such accuracies on the data analysis.

An analytic representation of the variation of aerodynamic coefficients, particularly axial force coefficient, with Mach number should result in a substantial improvement in the speed and accuracy of the algorithm for processing the trajectory data. The results of an investigation of analytic functions used to represent such variations are discussed in Section 2. The results of testing the programs for analysing yawsonde and radar data are discussed in Section 5. The two principal points of interest are firstly, the advantages of using an analytic representation of Mach number variation compared with the

commonly used method of analysing a section of data restricted so that the Mach number variation over that section is not significant, and secondly, the effect on the parameter estimation process of noise in the data. Section 3 discusses the method for analysing the trajectory data and gives details of the operation of the program SHELTRAJ, which is used to implement it. The factors affecting the design of experiments involving yawsondes are summarised in Section 4, which also describes the method of analysing the yawsonde data, and the operation of the program YAWSONDE. The final section discusses the design of experiments using radar tracking, yawsondes, or both. It also looks at the present state of progress and considers which direction future work should take.

2. ANALYTICAL REPRESENTATION OF THE VARIATION OF AERODYNAMIC COEFFICIENTS WITH MACH NUMBER

In analysing data from free flight trials, the methods generally used involve the assumption that aerodynamic coefficients are not Mach number dependent. In a few cases a linear variation is allowed(ref.9). The variation of aerodynamic force and moment coefficients with Mach number is taken into account in using these methods by restricting the data analysed in any one pass to a section in which the Mach number variation is so small that there will not be a significant variation in any of the aerodynamic coefficients extracted. There are several obvious disadvantages of this system. The major drawback is the difficulty of obtaining information in the transonic region where the axial force in particular is changing rapidly. Thus in the transonic range it is difficult if not impossible to find a sufficient length of trajectory over which drag coefficient can be adequately represented by a constant or a linear variation with Mach number.

The slowly varying nature of the tracking data from which the aerodynamic forces are derived and the roll rate data from which roll damping is obtained, necessitates using as long a section of the trajectory data as possible. rapid oscillatory nature of the angular data means that the aerodynamic moments can be determined from much shorter sections of the trajectory so that it is not necessary to use a sophisticated representation of the variation of aerodynamic moments with Mach number. Therefore an analytic form for the variation of axial force coefficient with Mach number will be used, and in addition analytic representations will be used for other slowly varying quantities, namely, average normal force and roll damping. Then the data analysis method will make optimum use of the data, and much more accurate estimates of the aerodynamic parameters will be obtained. In particular, the best estimates of axial force will be obtained, and this is most important if the technique is to be useful in setting up a Fire Control Model.

In order to choose an analytic form to describe the variation with Mach number of the three coefficients, that is, the axial force coefficient, the normal force coefficient and the roll damping coefficient, some experiments were conducted in fitting analytic forms to typical aerodynamic coefficients for a shell. Tabulated values which were used in this exercise are shown in Table 1.

2.1 Axial force

The transonic drag rise is such that polynomial representations of the Mach number variation of axial force coefficient are always poor. Criteria for choosing a suitable analytic function can be found in reference 10 and have been repeated in Appendix I, which gives details of the functional form proposed in reference 10. The principal advantage of this function lies with the small number of parameters necessary to provide adequate representation of the axial force coefficient, over the whole Mach number range. The function, which will be called the NR3634 drag function, has the form

$$C_{x} = (1+s)A(r) + (1-s)B(r)$$

where A(r), B(r) are polynomials and r, s are functions of Mach number,

$$r = (M^2 - K^2) / (M^2 + K^2),$$

 $s = r / [(1 - L^2) r^2 + L^2]^{\frac{1}{2}}.$

A detailed discussion of the function, its properties and the values of the constants can be found in reference 10. A possible alternative is the Gavre drag function(ref.11), which is slightly more complex than the NR3634 function but otherwise has the same advantages. The Gavre drag function has the form

$$C_{X} = a + [1 + b(M-c)^{2}] tan^{-1} \{d(M-c) / [e + f(M-c)^{2}]\}$$
.

In order to choose the more appropriate analytic form for incorporation into the data analysis a short study of the goodness of fit of each form was carried out for the tabulated axial force coefficient in Table 1. A nonlinear least squares method was used to fit the curves to the data. of squares of the differences between the tabulated values and those derived from the analytical representation was minimised, using the subroutine given in reference 13, which implements the method described in reference 12. results of the study are given in Table 2 and figure 1. The fitting was carried out over the Mach number range from 0.65 to 1.4 since this particular shell will not be subject to Mach numbers outside that range except in exceptional circumstances. From part (a) of Table 2 it is clear that the optimum fit is obtained using linear polynomials in r to represent both supersonic and subsonic parts of the curve. This result is optimum in the sense that it involves using the least number of adjustable parameters and yet results in a very small r.m.s. error for the fit. If more parameters are used the root mean square error of the fit does not decrease substantially. Coincidentally the number of parameters for optimum use of the NR3634 drag function is the same as the number of parameters used with the Gavre drag function, namely, six. However, the root mean square error attained with the NR3634 drag function is less than one fifth of that obtained with the Gavre drag function, so that the choice is quite clear cut. drag functions have basically the same shape, which includes in particular a rapid rise in the transonic region, this preference can be expected to hold generally. Figure 1, which shows the drag variation with Mach number and the residues obtained with the various fitted curves supports this It is particularly noticeable that the Gavre drag function has difficulty coping with the transonic drag rise. The error peaks at M = 0.93and M = 1.02 show an inability to cope with the high curvatures at these points which are a feature of the transonic drag rise. These results contrast with the residues shown for the NR3634 drag curves, of which one uses a constant and the other uses a linear representation to describe the subsonic part of the curve. Both are linear supersonically.

It was concluded from this study that the NR3634 drag curve using linear functions of r both subsonically and supersonically would represent the axial force curve adequately over the Mach number range used by shells in flight. However provision was made in the parameter estimation program for analysing the radar data to use up to quadratic terms to cope with exceptional cases if they arise.

2.2 Normal force derivative

Since the NR3634 drag function provides such an excellent representation of the axial force and since the normal force coefficient derivative has similar characteristics to the axial force coefficient, in particular a rapid increase in magnitude in the transonic region, then the NR3634 function is an appropriate choice for analytic representation of the normal force coefficient derivative. Details of the results of fitting such a function to the values of normal force coefficient derivative given in Table 1 are presented in figure 2 and Table 3. Again fitting has only been tried for the Mach number range 0.65 to 1.4. It is clear from the table and figure that an NR3634 curve using linear representations both subsonically and supersonically provides quite adequate representation of the normal force while using only six parameters. The deviation of the analytic representation from the tabulated curve will be less than half a per cent at its maximum value and Since the effect of normal force on the shell is generally very much less. principally involved with the drift of the shell, such accuracy is more than Therefore an NR3634 curve can provide an adequate representation of the normal force coefficient derivative, using a linear form both subsonically and supersonically. Again provision is made in the parameter estimation program SHELTRAJ to use up to quadratic terms if necessary, but such a requirement is unlikely and it would be difficult, if not impossible, to determine values for the extra parameters.

2.3 Roll damping derivative

Unlike the force coefficient, the roll damping coefficient derivative does not change rapidly in the transonic region, but shows a small steady variation over the whole Mach number range. Consequently, a polynomial representation Table 3(b) and figure 3 show the results of fitting is perfectly adequate. polynomials to the tabulated values in Table 1, using a linear regression Figure 3 shows the magnitude of the residuals obtained, using technique. both linear and quadratic variations and Table 3(b) shows the r.m.s. errors for polynomials up to and including the fourth degree. The fitting was done over a Mach number range from 0 to 2.5 using all the points tabulated in Table 1. The decrease in the sum of squares of the residuals as the degree of the polynomial increases is a useful measure of the improvement in fitting to the data of the higher degree polynomial. It follows that the results in Table 3(b) show that no significant improvement can be achieved with polynomials of degree higher than four and that a quadratic representation is quite adequate, since the residuals of the quadratic form are less than one Hence provision is made in program SHELTRAJ to use up to third degree polynomial representations of the derivative of the roll damping moment coefficient. However, a quadratic will generally be adequate, and in many cases with a restricted Mach number range, a linear representation will be sufficient.

3. TRAJECTORY DATA ANALYSIS

The trajectory data analysis and the yawsonde data analysis can be viewed as entirely separate and unconnected processes and both can be undertaken together or each can be undertaken in isolation. Analysis of the trajectory data obtained by radar tracking or flashing light measurement will be the basis of any method, which might be developed for producing a Fire Control Model. The mathematical model which is used as a basis for the parameter estimation is the four degree of freedom or modified point mass model proposed by Lieske and Rieter(ref.3). The algorithm is similar in many ways to the methods already in use(refs.7,9). The basic difference is that both of the above methods treat

only a length of the trajectory which is limited so that the Mach number range is sufficiently small for the variation of aerodynamic coefficients with Mach number to be adequately represented by constants or straight lines. On the other hand the method described below will process the whole trajectory in one sweep using the analytic representations of aerodynamic forces and rolling moments described in Section 2. In addition to describing the mathematical model used in the program, this section outlines the parameter estimation algorithm, describes the program SHELTRAJ itself and provides a brief description of the method for using it and the input to and the output from the program.

3.1 Mathematical model

The mathematical model allows for motion with respect to the three translational degrees of freedom and the axial spin or roll degree of freedom, and so is generally called a four degree of freedom trajectory model. The model relies on the fact that for a well behaved shell, an accurate prediction of the shell drift, that is, the lateral displacement of the shell's impact position from that given by a point mass trajectory model, can be made by assuming that the shell flies at the yaw of response. The yaw of response of a shell is the equilibrium value of incidence when transient yawing and pitching moments are damped out. For most shells the yaw of response is close to the horizontal plane and its magnitude can be approximated by the expression

$$\xi_{R} = p_{s}I_{x} V_{1} g_{3} / QSdV^{2} C_{m\xi}$$
 (1)

The axes system in which the equations of motion are formulated is a range axes system. It has OX downrange along the line of fire, OY to the right and OZ vertically downwards to complete a right handed set. The velocity in the range axes system is

$$U = \dot{x}\dot{1} + \dot{y}\dot{1} + \dot{z}\dot{k} ,$$

where i, j, k are unit vectors in the X, Y and Z directions respectively. The equations of motion for the shell at the yaw of repose, are

$$\dot{\underline{U}} = -(QSC_{x}/m) \underline{v} + (QSC_{L}/m) \underline{j} + \underline{g} - \underline{\Lambda}$$

$$\dot{p}_{s} = (QSd/I_{x}) (p_{s}d/2V) C_{\ell_{p}},$$
(2)

where v is a unit vector in the direction of the shell velocity relative to the air, so that

$$\underline{V} = |\underline{V}|\underline{v} = \underline{U} - \underline{W}$$

where W is the local wind velocity and V has components (V_1, V_2, V_3) in range axes. The drag and lift coefficients shown in equation (2) can be expressed in terms of axial force and normal force as follows,

$$C_{D} = -C_{x} \cos \xi - C_{z} \sin \xi , \qquad (3)$$

$$C_{L} = C_{x} \sin \xi - C_{z} \cos \xi .$$

The resolution of the aerodynamic forces of lift and drag into axial and normal force is not generally necessary. In fact, if the sole purpose of the data analysis were the development of a Fire Control Model the use of lift and drag forces would be preferable. However, since the more significant aspect of the present development is a general study of stability and the program is intended for use in the yawsonde data analysis program as well, it is advantageous at this stage to use a formulation which is in terms of axial and normal force. The remaining symbols in the above equations are standard and are defined in the list of notation at the end of the text. The gravity and Coriolis acceleration terms are discussed at length in Appendix II.

Small approximations have been used in equations (1) and (2). In equation (1) the vertical component of the yaw of repose has been ignored and an approximate expression has been used for the magnitude of the horizontal component. The errors arising from both approximations will have maximum values of only one or two per cent of the total yaw of repose and so it is expected that this approximation will not affect the results significantly. In equation (2), the direction of the lift force has been taken along the vector j. This is true at the beginning of the trajectory if there is no wind, but the direction will alter slightly with cross wind present and as the shell drifts slightly from the line of fire. Once again the overall errors arising from this approximation will not generally be significant.

The final part of the mathematical model is the parametric representation which enables the implementation of the parameter estimation algorithm. Firstly, we consider initial values of the variables

$$P_1 = x_0, P_2 = y_0, P_3 = z_0$$
 (4)
 $P_4 = \dot{x}_0, P_5 = \dot{y}_0, P_6 = \dot{z}_0 \text{ and } P_{27} = P_{SO}.$

The parametric representations of the aerodynamic forces and the roll damping moment include the axial force coefficient which is represented in the following way, using the functional form presented in Section 2,

$$C_x = (1+s) (P_9 + P_{10}r + P_{11}r^2)$$

+ (1-s) $(P_{12} + P_{13}r + P_{14}r^2)$ (5)

where

$$r = (M^2 - P_7^2) / (M^2 + P_7^2),$$

 $s = r / [(1 - P_8^2) r^2 + P_8^2]^{\frac{1}{2}}.$

The normal force coefficient derivative is represented using the same type of function as follows,

$$C_{Z_{5}^{\prime}} = (1+f) (P_{17}+P_{18} g+P_{19} g^{2}) + (1-f) (P_{20}+P_{21} g+P_{22} g^{2})$$
 (6)

where

$$g = (M^2 - P_{15}^2) / (M^2 + P_{15}^2),$$

$$f = g / [(1 - P_{16}^2) g^2 + P_{16}^2]^{\frac{1}{2}}$$

Finally, a simple polynomial representation is satisfactory for the derivative of the roll damping moment coefficient, having the form

$$C_{\ell_p} = P_{23} + P_{24}^M + P_{25}^{M^2} + P_{26}^{M^3}$$
 (7)

Thus equations (1) to (7) completely define a mathematical model describing a four degree of freedom or modified point mass model of a shell trajectory in terms of the 27 unknown parameters P_i . In most cases it will not be necessary to determine values for all the parameters. Firstly, some or all of the initial conditions may be sufficiently well determined by other means and so they can be kept fixed throughout the data analysis. Secondly, the variation of the aerodynamic coefficients with Mach number may be adequately represented by fewer parameters than are available, particularly when the available data covers only a restricted range of Mach number. Then the less significant parameters can be set to zero and held constant.

The parameter estimation process which is used to assign values to the unknown parameters P_i is a minimum variance technique. The minimum variance estimator aims to find values of the parameters which will minimise the weighted sum of the squares of the residuals, of the measured values of the three position coordinates and the roll rate when compared with the values predicted by the model. The method is described in detail in references 4, 5 and 8. It is basically a modified Newton-Raphson algorithm and as such it needs an estimate of the partial derivatives of each of the measured variables with respect to the parameters. A means of derivation for these partial derivatives is given in Appendix III.

The interaction between position and roll rate data is minimal. Since the only connecting variable is yaw of repose it is very difficult and often impossible to determine simultaneously, parameters affecting aerodynamic forces directly and those affecting rolling moments directly. In order to determine them separately, use can be made of the fact that in determining minimum variance the residuals are weighted, that is,

$$\sigma^{2} = (1/4N) \sum_{j=1}^{N} [w_{1} (\hat{x}_{j} - x_{j})^{2} + w_{2} (\hat{y}_{j} - y_{j})^{2}]$$

+
$$w_3 (\hat{z}_j - z_j)^2 + w_4 (\hat{p}_j - p_j)^2$$
].

Then aerodynamic force parameters, P_i for i=1 to 22 and aerodynamic rolling moment parameters, P_i for i=23 to 27 can be determined separately, using $w_k \neq 0$ for k=1, 2, 3 and $w_4=0$, when forces are required and $w_1=w_2=w_3=0$, $w_4\neq 0$ when rolling moments are required. The choice of appropriate values for the w_i is discussed further in Section 3.2.1 on input to the program.

3.2 Program SHELTRAJ

The mathematical model and parameter estimation algorithm are implemented by the computer program SHELTRAJ. A listing of the program is given in This section discusses input, output and usage of the program. The program consists of a main program and thirteen subroutines. program controls the input, output, solution of equations of motion and adjustment of parameter values by iteration. There are sets of routines controlling input/output, setting up and integrating the mathematical model equations by a fourth order Runge Kutta method, and implementing the parameter Function routines define the Kronecker delta and the estimation algorithm. pitching moment derivative at zero incidence, for the shell under considera-The pitching moment derivative is used in equation (1) to estimate the yaw of repose. The need for this can be avoided by formulating the parameterised mathematical model equations (2) to (7) in terms of drag and lift rather than axial and normal force. Then C, in equation (2) is given by

$$C_{L} = C_{L\zeta}\zeta = (p_{s}I_{x}V_{1}g_{3}/QsdV^{2})(C_{L\zeta}/C_{M\zeta})$$
 (8)

so that the ratio $(C_{L_X^c}/C_{M_X^c})$ can be included in the parametric representation in equation (6) in place of $C_{Z_X^c}$ and the parametric representation in equation (5) can be used for C_D rather than C_X . This course would be preferable if the program were for use in constructing a Fire Control Model, where the separation of C_X , $C_{Z_X^c}$, $C_{M_X^c}$ is not necessary, since shell trajectories are calculated simply using the mathematical model and the estimated parameter values. When yawsonde data, which will provide independent estimates of $C_{M_X^c}$, is available then the approach employed in SHELTRAJ is more useful, since it provides a better description of the behaviour of the shell.

3.2.1 Input

Three logical units, 3, 5 and 8 are used to input all the data to program SHELTRAJ. The input required from unit 5 either as cards or card images is described in Table 4, and two examples of such input decks are shown in Table 5. The variables LENTER and LCASE are used to control a facility for multiple runs. When LCASE is non-zero control returns to the beginning of the card input on run completion. Then by using LENTER, control can be transferred to any one of several points in the input stream and the run repeated with new values for selected variables.

Several facilities are available in choosing values for input variables to provide the user with fine control on the parameter estimation algorithm. The array JORDER, allows the user to set the order of priority of the parameters so that if JORDER(i)=j then the ith parameter in the mathematical model defined above will be placed in the jth position in the reordered set. The most reliable strategy for obtaining convergence is to approach the solution piece-The technique involves allowing only a few parameter values to vary initially and then repeating the run several times with a gradually increasing number of parameters varying. This is achieved by arranging the parameters in order of importance using JORDER, then gradually increasing the value of NPARAM with repeated runs until values have been estimated for all the desired parameters.

During execution, after the first iteration, the measured variable values are compared with the mathematical model outputs and if the differences between the two are greater than four standard deviations for any element of the measurement vector then that measurement is rejected because it is considered to be a rogue. During the first iteration no estimate of the standard deviation is available and so a value for the data rejection level, REJECT, must be supplied by the user. It is generally good policy to choose a large value so that few, if any, points will be rejected on the first iteration.

As we will discover below it is often difficult, if not impossible, to determine parameters defining aerodynamic forces and those defining rolling moments simultaneously. Separating the two problems can be achieved by means of the weighting factors XS. To estimate force parameters we set XS(1), XS(2), XS(3) at non-zero values and XS(4) = 0, while to estimate the rolling moment parameters we set XS(1) = XS(2) = XS(3) = 0 and XS(4) = 1. Tables S(a) and S(b) show data decks designed to implement the two types of calculation. In general values of the weighting factors XS(1) are chosen in proportion to the relative accuracies of each component of the measurement vector.

In addition to the input from unit 5, the program uses experimental data from unit 3 and meteorological data from unit 8. The experimental measurements should be in 5E16.8 format and each record should contain one value of each of time, x, y and z coordinates in range axes, and roll rate. Input begins at the first data point with time greater than TO and every ISKIP th point is read until a total of NPTS points is reached. Finally meteorological data is input as described by the control variable IND. There are two types of table for the meteorological data and they use a 3F10.0 format. Each record contains only one table entry consisting of three items and each table may have up to 150 entries. Each entry in the wind table contains altitude above range origin, range wind, which is positive downrange and crosswind, which is positive to the right, while each entry in the pressure temperature table contains altitude, pressure in pascals and temperature in degrees Kelvin.

3.2.2 Output

The output from the program SHELTRAJ consists basically of a record of the input data, successive values of the parameters as they are adjusted at each iteration, together with r.m.s. errors in each parameter. When convergence is achieved the final parameter values and the covariance matrix are printed. The model outputs and the residuals of the measured values can be both printed and plotted if requested by using a non-zero value of NPLOT in the input.

Artificially produced data from a six degree of freedom model of the shell behaviour is shown in Table 6. This data has been used in conjunction with the data decks in Table 5 to test the program extensively. The results of these tests will be discussed in Section 5. Excerpts from the beginning and the end of the outputs for each data deck appear in Table 7.

4. YAWSONDE DATA ANALYSIS

The yawsonde was developed in the early 1960s(ref.1). Since then several significant improvements have been made to the original design(ref.2). The yawsonde measures the complementary solar aspect angle, which is the angle between the normal to the longitudinal axis of the shell and the direction of the sun. Figure 4 shows a schematic representation of the yawsonde and the angles associated with it.

As the yawsonde measures only the angle between the shell axis and the sun direction it provides essentially only a one-dimensional picture of the angular motion of the shell, which is basically two-dimensional. For this reason the use of yawsondes to study flight behaviour of shells was quite limited for many years. However, the recent application of parameter estimation to the problem has greatly increased the potential of yawsondes with regard to analysing the flight behaviour of shells. Provided that there is a significant component of the angular motion in the plane defined by the instantaneous velocity vector and the direction of the sun, parameter estimation can be used to reconstruct the total motion.

The following subsections deal with the factors which need to be taken into account in designing experiments with yawsondes, the mathematical model on which the data analysis is based, and the use of the program YAWSONDE which is designed to carry out that data analysis. An important aspect of the analysis of the yawsonde data is the piecemeal approach. This change is due to the much higher frequencies of those components of the motion measured by the yawsonde, that is, nutation and precession, compared with the components discussed in the previous section. Because of the higher frequencies the required parameters can be determined from much shorter lengths of data. Hence the restriction of data analysis runs to sections of the trajectory over which variations in Mach number are not significant, is no longer a problem so that the piecemeal approach, which severely limits analysis of the trajectory data, is quite adequate for analysing yawsonde data.

4.1 Yawsonde usage

The yawsonde is depicted schematically in figure 4. It consists of two slits containing sun sensors at two points on the circumference of the shell. The longitudinal plane of each slit makes a specified angle with the longitudinal axis of the shell. As the shell rotates, the yawsonde produces a pulse train of the type shown in figure 4, with pulses of different polarity from each sensor. The relationship between the pulse train and the angle between the direction of the sun and the normal to the longitudinal axis of the shell, that is, the complementary solar aspect angle, is derived Since the angles γ_1 , γ_2 and β are nominal values only and in Appendix V. cannot be reproduced exactly in the real yawsonde, and since the theoretical relationship derived in Appendix V does not take account of the finite displacement of the slits from the origin of the axes system, the yawsonde must One method of calibration is described in reference 2. be calibrated. Any such method involves a series of measurements of the corresponding values of τ/T and σ_N as they appear in equation (22). In order to smooth measurement errors and obtain an analytic calibration curve which can be used later to process the experimentally measured values of τ/T , we obtain values of the parameters γ_1 , γ_2 and β using a nonlinear least squares fitting technique similar to that described in Section 2. A listing of the program YAWCAL, which is used to do the fitting, appears in Appendix VI. required by the program is described in Table 8. The program us The program uses a minimisation routine from reference 13 which is based on the method of Fletcher Figure 5 shows a typical calibration curve for a and Powell (ref.12). yawsonde. The main features which are worth noticing are the sensitivity at $\sigma_{N} = 0$ and the limitations on the measurement range. If we use the commonly chosen nominal values $\gamma_1 = -\gamma_2 = \gamma$ and $\beta = \pi$ for the angles defined in figure 4 where γ is usually chosen near $\pi/4$, the expressions in Appendix V show that the measurement range is

and the sensitivity at $\sigma_N = 0$ is

$$d \sigma_{N}/d (\tau/T) \mid_{\tau/T=\frac{1}{2}} = \pi/\tan \gamma$$
.

This means that the sensitivity deteriorates rapidly as γ increases beyond $\pi/4$ so that a useful value of γ is somewhere in the range $\pi/6$ to $\pi/4$. The value in the examples in figures 5, 6 and 7 is $\pi/4$.

The limited range of measurement means that care must be exercised in trials planning to keep the complementary solar aspect angle within the range that the yawsonde can measure accurately. Care should be taken to avoid approaching the limits + $(\pi/2-\gamma)$ too closely because the finite physical dimensions of the slits render the calibration curves unreliable near those limits.

In order to use the yawsonde effectively we need to estimate the position of the sun. The method for estimating the azimuth and elevation of the sun in earth axes is given in Appendix VII together with an expression for the complementary solar aspect angle. For trials planning purposes we assume that the azimuth of the shell is the same as the bearing of the line of fire, since the difference between the two is generally quite small. ASPECT uses the results quoted in Appendix VII to estimate the complementary solar aspect angles at a range of times and elevation angles of the shell for a given day, place and line of fire. A listing of the program ASPECT may be Details of the input required by the program are found in Appendix VIII. given in Table 9. Two sets of results are given in figure 6 for this type of calculation for a shell fired at the Woomera Range on the 15th of March The results are given for directions of firing with bearings of 300 degrees and 0 degrees from true north. The range of angle which can be measured with the yawsonde, $-\pi/4$ to $\pi/4$ in this example, is shown by the dashed line. It is clear from these two figures that in order to obtain complete coverage of the trajectory, particularly for high elevations, it is necessary to fire nearly due north or nearly due south early in the day. In order to get a clearer picture of the optimum firing conditions the results have been presented slightly differently in figure 7. shows an example of the range of elevation angles of the shell for which the yawsonde can detect the sun, as a function of time of day and bearing of the line of fire. The elevation angles on the shaded side of the curve are outside the range. It is apparent from the figure that the whole range of elevation angles can only be covered by firing sufficiently close to due north before 0930 or near enough to due south before 1100. Only the morning hours are covered in this figure, but similar conditions prevail in the late afternoon, when the whole range of elevation angles can be covered again by firing sufficiently near due north or due south. If we are prepared to sacrifice most of the downward leg of the trajectory, that is, negative elevation angles, and the firing elevation is not too high, then there is a much wider choice of firing conditions. For example, if a shell is fired at an elevation of 40 degrees and the trajectory is only required down to -10 degrees, then the firing can take place any time between 1100 hours and 1300 hours on a bearing between 110 degrees and 280 degrees. Alternatively, if the line of fire is fixed and some part of the trajectory can be sacrificed, there is generally a period during the day when the firing can be carried out and a satisfactory coverage of the trajectory obtained.

4.2 Mathematical model

In analysing the data from measurements made with a yawsonde we are interested primarily in the two angular degrees of freedom, pitch and yaw, which are neglected in the four degree of freedom mathematical model used in analysing the trajectory data. The four first order equations which define the angular pitching and yawing motion of the shell are

$$\dot{\psi} = r \sec\theta ,$$

$$\dot{\theta} = q ,$$

$$\dot{q} = pr - (I_{x}/I) p_{s}r + (QSd/I) [C_{m}\cos\phi - C_{np} (p_{s}d/2V) \sin\phi + C_{mq} (qd/2V)] ,$$

$$\dot{r} = -pq + (I_{x}/I) p_{s}q + (QSd/I) [C_{m}\sin\phi + C_{np} (p_{s}d/2V) \cos\phi + C_{mq} (rd/2V)] .$$
(9)

The equations are formulated in an aeroballistic axes system, which is constrained to pitch and yaw with the vehicle and to maintain the GY' axis horizontal. Hence the GX' axis is forward along the horizontal axis of the shell; the GY' axis is horizontal and the GZ' axis is such that GX'Z' is a vertical plane. Then the roll rate of the axes system must be given by

$$p = -r \tan\theta \tag{10}$$

The roll rate of the shell, p_s , the velocity, V, and the dynamic pressure, Q, can all be obtained from the trajectory data analysis, discussed in Section 3. Apart from the aerodynamic coefficients and the angle ϕ , which are discussed further below, the remaining parameters in equation (9) all represent physical characteristics of the vehicle which can be measured before the trial.

If this mathematical model is to be used in the parameter estimation process, then a parametric representation of the unknown quantities which appear in these equations has to be formulated. Firstly, consider the initial values of the variables; they are represented as follows,

$$\psi_0 = P_1, \theta = P_2,$$
 $q_0 = P_3 \text{ and } r_0 = P_4.$ (11)

The other unknown quantities in equation (9) are the aerodynamic coefficients. The following representation has been used for them

$$C_{m} = (P_{5} + P_{12}M)\xi + P_{6}\xi^{3} + P_{7}\xi^{5} ,$$

$$C_{np} = P_{8}\xi + P_{9}\xi^{3} ,$$

$$C_{mq} = P_{10} + P_{11}\xi^{2} .$$
(12)

If, ζ is the magnitude of the angle of attack and ϕ is the orientation of the plane of the angle of attack then they are defined by the relations

$$\tan \zeta = (v + w)^{\frac{1}{2}} / |u|$$
, (13)
 $\tan \phi = (-v) / w$,

where (u, v, w) are the components of the true air velocity in aeroballistic axes. They are defined in terms of the range components of vehicle velocity which are obtained from analysis of the trajectory data, by the transformation

$$\begin{bmatrix} \mathbf{u} \\ \mathbf{v} \\ \mathbf{w} \end{bmatrix} = \begin{bmatrix} \cos\theta & \cos\psi & \cos\theta & \sin\psi & -\sin\theta \\ -\sin\psi & & \cos\psi & 0 \\ \sin\theta & \cos\psi & \sin\theta & \sin\psi & \cos\theta \end{bmatrix} \begin{bmatrix} \mathbf{v}_1 \\ \mathbf{v}_2 \\ \mathbf{v}_3 \end{bmatrix}$$
(14)

Equations (9) to (12) comprise a mathematical model of the portion of the behaviour of the shell which affects the yawsonde measurements, in terms of the unknown parameters, P_i . The criterion used to estimate values for the parameters is to minimise the average of the sum of squares of the residuals

$$\sigma^2 = \frac{1}{N} \sum_{j=1}^{N} (\hat{\sigma}_{Nj} - \sigma_{Nj})^2$$

where $\hat{\sigma}_{Nj}$ is the measured value of the complementary solar aspect angle and σ_{Nj} is the value predicted by the mathematical model. The value of σ_{Nj} is estimated by substituting the value of the local time at which the trial occurred and the values of ψ and θ predicted by the mathematical model into the relations given in Appendix VI.

The parameter estimation algorithm is the same as that used in the trajectory analysis and described in detail in references 4, 5, 8 and 9. The algorithm uses partial derivatives of the complementary solar aspect angles with respect to the parameters to obtain adjustments for each parameter value during each iteration. These partial derivatives are obtained by numerical integration of equations which are derived from the mathematical model equations by partial differentiation. Details of the derivation of the partial derivatives are given in Appendix IX.

4.3 Program YAWSONDE

The parameter estimation processing for the yawsonde data is implemented in the computer program YAWSONDE. A listing of the program may be found in Appendix X. The program consists of a main program and eleven subroutines. The main program controls the processing of the data by the routines. The subroutines fall into three categories which serve the functions of input and output, numerical integration of the differential equations to simulate shell behaviour and estimate values of partial derivatives and finally, the calculation of adjustments to the parameter values using the parameter estimation algorithm.

4.3.1 Input

Details of the input needed from unit 5 either as cards or card images are provided in Table 10, and an example of such a deck appears in Table 11. The controls for the parameter estimation process are the same as those used by SHELTRAJ. They are discussed in detail in Section 3.2.1, and therefore will not be discussed here. The meteorological data is also the same as that for SHELTRAJ and a detailed description of this also may be found in Section 3.2.1.

The major differences from the input requirements of the program SHELTRAJ are the specification of sun position and trajectory data and the experimental measurements. There is provision to tabulate variation of the direction cosines of the sun as a function of time along the trajectory. If this is not deemed necessary constant average values can be entered with times corresponding to the beginning and end of the trajectory as has been done in the example in Table 11. The trajectory data which is needed to estimate such things as dynamic pressure, velocity and so on, in the mathematical model equations must be supplied in a separate input dataset on unit 4. usually be obtained from the smoothed trajectory produced by the analysis The program will read from the dataset a described in Section 3. total of NTRAJ points on the trajectory, using only every ISKIP th point in the dataset, where NTRAJ and ISKIP are input from unit 5. The records in the dataset should have 8F10.0 format and each record should contain values of time, range velocity, drift velocity, which is positive to the right, vertical velocity, which is positive downwards, altitude and roll rate. Finally the experimental data is input from a dataset attached as unit 3. The first data point is that for the first time greater than TO. Every ISKIP th point is input until a total of NPTS points is reached. Values for TO, ISKIP and NPTS are all read from the cards described in Table 10. Each experimental record is in 2E16.7 format and contains a value of time and the complementary solar aspect angle in radians.

4.3.2 Output

The output from YAWSONDE is similar to that from SHELTRAJ. It consists principally of a record of the input data, values of parameters and their estimated errors after each iteration and the covariance matrix when convergence is achieved. Model outputs and residuals of the measured values can be both printed and plotted by assigning a non-zero value to NPLOT.

Artificially produced data relating to trajectory and yawsonde measurements is given in Table 12. This has been used in conjunction with the card deck in Table 11 to test the program. The beginning and end of the output from this test run is given in Table 13. The more significant aspects of the results from the program testing are discussed in detail in the next section.

12

5. PROGRAM TESTING

Both programs were tested using simulated data obtained from a six degree of freedom trajectory model which used linear interpolation amongst the tabulated values of the aerodynamic coefficient given in Table 1. Listings of the simulated data appear in Tables 6 and 12. Test cases were run both with and without Gaussian white noise superimposed on the data for each program. Tests were also run with the trajectory data to compare the efficiency of the program SHELTRAJ with a method which allowed only a linear variation of drag with Mach number and kept all other coefficients constant. Details of the results of these test runs are given below.

5.1 Program SHELTRAJ

The testing of SHELTRAJ fell naturally into two areas, one involving the aerodynamic forces and the other involving the aerodynamic moments, specifically the roll damping moment. The determination of aerodynamic forces will be discussed first. It proved impossible to determine all the parameters defining the forces even using the clean data. However, only the subsonic part of the curve for the normal force derivative was troublesome. The initial conditions, the drag force coefficient and the supersonic part of the normal force derivative, a total of 16 parameters in all, were well determined. These parameters were the first 16 defined by the data deck in Table 5(a). The whole run occupied some 10 minutes of CPU time on the IBM 370/168 computer. However, it should be remembered that the whole trajectory was processed in that one run, whereas other methods would require at least 25 runs to process the same data.

The same test case was rerun with Gaussian white noise superimposed on each component of the data. The noise had a standard deviation of 5 m. The information extracted from this case was very limited. Only the axial force was obtained with any reliability at all, and the error in that approached 10 per cent in many places. This means that the r.m.s. noise level in each position coordinate would need to be much lower than 5 m if the application of parameter estimation methods to the analysis of trajectory

data were to be used in constructing a Fire Control Model.

In order to gauge the improvement in the data analysis which was achieved by using analytic functions of Mach number to represent aerodynamic forces, tests were run allowing only linear variation of axial force and keeping the normal force derivative constant, an approach similar to that used in The results of the testing of capabilities of the two methods reference 9. are shown in figure 8. Figure 8(a) shows the results for the axial force, comparing results obtained from the parameter estimation methods, using both noisy and clean data, with the curve used to generate the data from the six degree of freedom model. From analysis of uncontaminated data, the method proposed in Section 2 produced an analytic axial force curve which followed the original except at very low Mach numbers where there was no data because the section of trajectory which was analysed only covered Mach numbers from 1.37 down to 0.57. When the method was applied to noisy data the result contained errors as high as 8 per cent but generally followed the original fairly well. It should be noted that the noise model used represents an extremely noisy data collection method and modern tracking radars would produce a very much better signal. The tests with such poor data were aimed at determining the advantages of analytic representations of Mach number, and also the general capabilities of the method when radar data is poor. This aspect of the problem is discussed further in the next section.

By comparing the results from the present approach with those of the method of reference 9 one can elicit very definite conclusions. the axial force is concerned the method of reference 9 produced reasonable results when the data was uncontaminated, although it was unable to represent the high curvatures near Mach numbers of 0.9 and 1.1. However, the results using noisy data were quite hopeless, except around Mach 0.7 where the very large number of data points in a small Mach number range was sufficient to compensate for the effects of noise. Figure 8(b) shows the corresponding results for normal force derivative. Both methods gave reasonable results from uncontaminated data but were completely hopeless when noisy data was An interesting feature of the results shown in figure 8(b) is that the normal force derivative was consistently underestimated. The error ranges from two to five per cent and arises because data generated by a six degree of freedom model has been fitted by an approximate four degree of freedom model. It is not apparent whether the principal source of the

discrepancy is the approximate form used for the four degree of freedom model, or whether the discrepancy is mainly due to the use of the four degree of freedom model itself. This aspect of the problem is discussed further in Section 7, in connection with the possible use of program SHELTRAJ in constructing or improving a Fire Control Model.

Finally it should be noted that the average CPU time used in the computer runs implementing the method of reference 9 was 10 s so that if the axial force coefficient can be adequately represented over the range of Mach number covered by the whole trajectory with about thirty straight lines, then one might achieve a fifty percent saving in CPU time compared with the analytic functions method. However, the results for axial force coefficient, derived by the piecemeal approach are less accurate and the method is less robust in the presence of noise. Also, if more runs are needed, the CPU time advantage

will rapidly disappear.

Now let us consider the roll damping moments. Experiments with the program rapidly showed that aerodynamic force coefficients and aerodynamic roll damping coefficients could not be satisfactorily determined simultaneously and the method outlined in Section 3.2.1 was used to separate the two processes. Figure 9 shows the results of some test runs to gauge the effect of noisy data on the results obtained for the roll damping moment. The Mach number range covered by the data is from 0.63 to 1.37 and it is apparent from figure 9 that if a cubic expression is used to represent the variation of the roll damping moment coefficient with Mach number there is considerable deviation from the true results near the limits of the range. This deviation increases dramatically as the noise level in the data increases. examples shown in figure 9 include a quadratic curve obtained by least squares fitting to the original data given in Table 1. This curve, for which coefficients are given in Table 3, is a base against which we can evaluate the other results. Also shown are four curves obtained from applying parameter estimation to artificially generated data from a six degree of freedom model, one obtained using uncontaminated data and the other three using noisy The noisy data was obtained from the uncontaminated data by adding Gaussian white noise with r.m.s. levels of 1 and 10 radians respectively. For the data with the higher noise level, results are shown for both cubic and linear variations with Mach number. It is clear from the figure that high noise levels will result in large deviations near the ends of the Mach number range unless the degree of the polynomial is severely restricted. linear representation results in much lower overall errors when there are high noise levels in the data. It is generally true in all parameter estimation problems, that there exists a critical number of parameters for given noise levels in the data, such that increasing the parameters past that number introduces spurious trends into the results. This applies to most curve fitting problems and is particularly evident here because of the relative simplicity of the problem. Figure 9 shows that the derivation of roll damping moments will be quite accurate despite high noise levels in the data, provided that the degree of polynomial representation is appropriately The rolling moment is estimated to better than five per cent accuracy when there is a r.m.s. noise level of 10 radians in the data, if a linear representation is used for variation of the moment coefficient with Mach number.

The determination of the roll damping moment is still part of the program SHELTRAJ at this stage, and in this form it takes about 6 minutes of CPU time on an IBM 370/168 to determine one of the cubic curves shown in figure 9. However, it would be a relatively simple undertaking to separate out the portion of the program which deals with rolling motion and this should reduce the computing time to less than a minute.

5.2 Program YAWSONDE

The testing of the program YAWSONDE was rather unrealistic in some The data used, shown in Table 11, was generated from a simple undisturbed trajectory and so represented a very low amplitude oscillation. Hence even the results for uncontaminated data show errors of several per cent in the restoring moment. However, the parameter estimation algorithm converged, even when all twelve parameters were allowed to vary (Table 13). When noise was added to the data with a root mean square amplitude about twice that of the oscillation, the algorithm converged with five parameters varying, although the actual results obtained were meaningless. two important conclusions can be drawn from the testing of program YAWSONDE. Firstly, in designing experiments to obtain aerodynamic moments from yawsonde measurements, care should be taken to produce an oscillation of several degrees amplitude if the moments are to be determined accurately. the parameter estimation is remarkably robust in this case since it was possible to get convergence with extremely high noise levels in the data.

The program YAWSONDE is restricted to ranges of data where changes in Mach number do not significantly affect aerodynamic coefficients. However, as a result of the high frequencies present in angular oscillations, particularly nutation which can show frequencies around 20 Hz, much shorter ranges of data are needed to determine aerodynamic moment coefficients reliably. As a general rule the amount of data necessary to determine a value for a given parameter is of a length representing about two or three cycles of the component of the motion which is most affected by that parameter. Therefore this restriction will not generally present any problems. In addition, each test run took only about twenty seconds of CPU time. Hence the analysis will be economical of computing time even though many runs will be needed to cover the complete range of Mach number.

6. SUMMARY OF RESULTS

The program SHELTRAJ, which was developed to analyse radar tracking and roll rate data is based on the concept of using analytic functions to represent the Mach number dependence of aerodynamic forces and rolling moments. Testing of the program demonstrated that this approach has potential for providing more accurate estimates of the relevant aerodynamic coefficients than a piecewise approach to the data analysis especially when there is a significant noise component in the data(ref.9). This result is particularly important in the context of using the technique to develop a Fire Control Model because highly accurate estimates of the axial force coefficient of a shell are needed in such a situation. The difficulties with estimating roll damping moments indicate that roll rate data should be analysed independently of the shell position data. This could be accomplished most efficiently using a completely separate computer program and removing altogether the facility for analysing roll rate measurements from SHELTRAJ.

The program YAWSONDE is very similar to other programs for analysing data on the complementary solar aspect angle. This particular version appears to be extremely stable. However, it is important to realise that the program will only provide an accurate estimate of the aerodynamic moments if the data being analysed covers a trajectory segment in which there is a pronounced incidence oscillation. Possible methods for generating the appropriate incidence oscillations are discussed in Section 7.

7. APPLICATION OF RESULTS

Many avenues for further investigation arose during the course of the work which has been reported here. Of these three particular areas are most likely to yield useful results. First let us consider improvements or changes to the programs developed to analyse both trajectory and yawsonde data. It is apparent from the work reported here that two improvements are particularly important. They are the development of a completely separate program to analyse roll rate data, and the formulation of the four degree of freedom model, which is used in the analysis of radar tracking data, in terms of the ratio of lift force derivative to pitching moment derivative. The idea of a separate program to analyse roll rate data was discussed at length in Section 5 where it was indicated that the CPU time used to process roll data could be substantially reduced by Initial trials indicate that the reduction is substantial and that less than ten seconds of CPU time will be needed, rather than several minutes. The use of the ratio of the derivatives of normal force and restoring moment was discussed in detail in Section 3.2 and the key equation (8) given. formulation of the problem is such that analysis of the trajectory data is Thus a Fire Control Model could be constructed completely self contained. from measurement of several trajectories without the need for wind tunnel data or a large number of range and accuracy firings.

A second avenue which needs further investigation is the connection between the amplitude of angular motions of the shell, accuracy capabilities of the yawsonde, and accuracy requirements for the aerodynamic coefficients which are derived from the measurements. Apart from studies applying the program to artificially manufactured data containing noise of known characteristics, studies will need to be made of methods for exciting angular motion in shells. Application of such methods would need to provide sufficient amplitude of shell yaw to satisfy accuracy requirements for the aerodynamic moment derivatives. Two methods which have been suggested are the introduction of an asymmetric mass distribution(ref.7) and the use of an asymmetrical muzzle brake(ref.18).

Finally, the data analysis method developed in Section 3 could be used extensively in the construction of a Fire Control Model. An investigation of the benefits of introducing parameter estimation techniques into the methodology for constructing a Fire Control Model should elicit many useful results. Several factors would need to be considered, such as the number of firings which would be necessary, the accuracy with which shell position would have to be measured, the possibility of using flashing lights rather than radar to measure position, how accurate the meteorological data would have to be and so on. aspect of the method of Section 3 which would definitely require further investigation is the use of the four degree of freedom model and the approximations which were used in equations (1) and (2) to make them tractable in the In fact further study of these approximations may be worthabove application. while in its own right, particularly since they are suspected of causing errors The question of the four degree of freedom in the estimates of the lift force. or modified point mass model is different altogether and it may be a definite advantage of the technique. In general, the Fire Control Model uses a four degree of freedom representation to calculate aiming data, because a more complex model is too difficult to implement on a field computer and too expensive of computing time. The four degree of freedom trajectory model is used in the reverse mode in the Model, from its application in the parameter estimation algorithm. Hence, while parameter estimates, obtained by fitting to several sets of trajectory data, may contain significant errors compared with wind tunnel measurements of the aerodynamic forces represented by them, the overall Model which is derived by this means is likely to be better than one which uses exact wind tunnel data. This follows because the parameter estimation process for construction of the Model would involve fitting the Model to

data from a wide range of trajectories, and so one would expect the Model to be extremely accurate when it is used in reverse to generate trajectories. Using such a method the development of a Fire Control Model would be faster and cheaper than at present, mainly because the number of range and accuracy firings would be substantially reduced. Hence, this is potentially the most useful application of the methods developed in this report, and therefore the most likely to repay further study.

NOTATION

A (r), B(r)	Polynomial functions in the NR3634 drag function
a	local speed of sound
a,b,c,d,e,f	coefficients of the Gavre drag function
a _n , b _n	coefficients of polynomials in the NR3634 drag function
c_{p}	aerodynamic drag force coefficient
c _L	aerodynamic lift force coefficient
c _x	aerodynamic axial force coefficient
C _{Yp} s	aerodynamic Magnus force derivative
cz	aerodynamic normal force coefficient, generally negative
CLS	aerodynamic lift force derivative
C _M ¢	aerodynamic normal force derivative
Cl _p	aerodynamic roll damping moment derivative
$^{\mathrm{C}}_{\mathrm{mq}}$	aerodynamic pitch damping moment derivative
C _{np}	aerodynamic Magnus moment derivative
d	maximum body diameter
f, g	variables used in NR3634 curve, representing normal force derivative, corresponding to the variables r, s used in representing axial force
$ g = \begin{bmatrix} g_1 \\ g_2 \\ g_3 \end{bmatrix} $	acceleration due to gravity in range axes
go	acceleration due to gravity at sea level
Н	hour angle of the sun
h	height of range origin, 0, above mean sea level
I _x	moment of inertia about the longitudinal axis
I	moment of inertia about the lateral axis
i, j, k	unit vectors in the range axes system
K	Mach number centred on the transonic drag rise for the NR3634 drag curve
L	width of the transonic drag rise for the NR3634 drag curve
М	free stream Mach number

m	mass of shell
N	number of data points
Na	degree of the polynomial used in the supersonic region of the NR3634 function ${\bf r}$
N _b	degree of the polynomial used in the subsonic region of the NR3634 function
P _i	unknown parameters in mathematical model
p _s	roll rate of shell
$\begin{bmatrix} \mathbf{p} \\ \mathbf{q} \\ \mathbf{r} \end{bmatrix}$	angular rates describing motion of the aeroballistic axes. Pitch and yaw rates are the same as those for the shell. Roll rate is such that the GY' axis remains horizontal.
$Q = \frac{1}{2} \rho V^2$	dynamic pressure
r	variable used in the NR3634 drag curve, $(M^2 - K^2)/(M^2 + K^2)$
r _o	radius of the earth
r	distance of the shell from the centre of the earth
S	maximum cross-sectional area of the shell
s	variable used in the NR3634 drag curve, $r/[(1-L^2) r^2 + L^2]^{\frac{1}{2}}$
T	period between pulses of like sign from the yawsonde, that is, roll period
t	time from the beginning of the shell flight
Ų	velocity of the shell relative to range axes. It has components $(\dot{x}, \dot{y}, \dot{z})$ in range axes.
V.	true air velocity of the shell. It has components (V_1, V_2, V_3) in range axes and (u, v, w) in aeroballistic axes. Magnitude is denoted by V.
v.	a unit vector in the direction of $\overset{V}{\sim}$.
₩.	wind vector, with components $(w_1, w_2, 0)$ in range axes.
w _i	weights used in forming the sum of squares of the residues of the data variables.
$\begin{bmatrix} x \\ y \\ z \end{bmatrix}$	denotes position in range axes, where OX is downrange, OY is horizontal to the right and OZ is vertically downwards. The origin O is generally at the gun

x' y' z'	denotes position in aeroballistic body axes, where Gx' is forward along the longitudinal axis, Gy' is horizontal to the right, and Gz' completes a right handed axes system. The origin G is at the centre of gravity of the shell.
[x"] y" z"]	Denotes position in rolling body axes with the origin S on the longitudinal axis of the shell at the location of the centre of the sun slits. Sx" is forward along the longitudinal axis, Sz" is outwards through the centre of sensor 1 in the yawsonde and Sy" completes a right handed set as shown in figure 4.
β	the circumferential angle between the two sensors in the yawsonde (see figure 4)
γ_1 , γ_2	the angles which the respective sensors in the yawsonde make with the longitudinal axis of the shell (see figure 4).
δ	declination of the sun
δ_{ij}	Kronecker delta, = 1 when $i = j$ and 0 otherwise
\$	total angle of attack
s _R	yaw of repose
Θ	latitude of shell
θ	elevation of the longitudinal axis of the shell
$\theta_{_{\mathbf{S}}}$	elevation of the sun
Λ ~	vector defining Coriolis force, with components (Λ_1 , Λ_2 , Λ_3) in range axes
ρ	local air density
σ	root mean square error in fitting the parametric model to the data
σ _N	complementary solar aspect angle, that is, the complement of the angle between the longitudinal axis of the shell and the direction of the sun.
τ	time between positive and negative pulses from the yawsondes (see figure 4)
Φ	longitude of the shell.
φ	orientation of the incidence of the shell relative to a vertical plane containing the longitudinal axis of the body. It is positive clockwise and is zero when the shell is nose up.
Ψ	bearing of line of fire relative to true north
Ψ	azimuth of the longitudinal axis of the shell

 $\psi_{\rm S} \qquad \qquad {\rm azimuth\ of\ the\ sun.}$ $\Omega \qquad \qquad {\rm angular\ velocity\ of\ the\ earth,\ with\ components} \qquad (\Omega_1,\Omega_2,\Omega_3) \ {\rm in\ range\ axes.}$ $0 \qquad \qquad {\rm partial\ differentiation\ operator.}$ Superscripts $. \qquad {\rm denotes\ differentiation\ with\ respect\ to\ time} \qquad {\rm denotes\ an\ experimentally\ measured\ value\ of\ a\ variable}$ Subscripts $0 \qquad {\rm denotes\ an\ initial\ value\ of\ the\ variable}$

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APPENDIX I

NR3634 DRAG CURVE

A brief resume of the properties of the formula, proposed in reference 10, to represent the variation of axial force over the entire Mach number range, is presented here to clarify comments on curve fitting and choice of values for parameters which are made in the main text.

The following criteria were used to construct the drag function defined below.

- (1) The function should effect some smoothing when fitted to experimental results. Hence the number of adjustable parameters, while being sufficiently large to provide adequate flexibility should be much less than the number of observations.
- (2) The function is empirical, but its behaviour should be consistent with basic characteristics of drag functions, such as asymptotic behaviour at high and low Mach numbers and transonic drag rise.
- (3) The analytic form should be simple and compact; transcendental and complex algebraic functions should be avoided.
- (4) The function should be analytic.
- (5) A simple procedure should be available for obtaining values of the parameters from experimental data.

Each of these conditions constitutes a considerable advantage over conventional methods of coefficient determination which rely on analysing only small portions of data during which the Mach number is almost constant. By repeating the analysis many times on different sections of trajectory such methods produce a table which shows variation of axial force with Mach number. Clearly an analytic representation which satisfies the above five conditions will result in greater accuracy and less computational effort in the analysis of position data for any trial.

The form for the analytic representation of the drag is

$$C_X = (1 + s)A(r) + (1-s)B(r)$$

where r,s are functions of Mach number,

$$r = (M^2 - K^2) / (M^2 + K^2)$$

 $s = r / [(1 - L^2)r^2 + L^2]^{\frac{1}{2}}$

and A(r), B(r) are both polynomials in r,

$$A(r) = \sum_{n=0}^{N_a} a_n r^n$$

$$B(\mathbf{r}) = \sum_{n=0}^{N_b} b_n \mathbf{r}^n$$

where a_n , b_n , K, L, N_a and N_b are constants to be determined.

The first property of the axial force coefficient function is explained by the result that K is close to 1 and L is small. Then for subsonic Mach numbers, M=0 upwards, r begins at -1 and approaches 0, somewhere in the transonic range and s is very close to -1 over the whole subsonic range, only changing appreciably when the transonic range is entered and $r \neq 0$. Hence, subsonically

$$C_{x} \approx 2B(r)$$
.

Somewhat similar effects occur supersonically, as $M \rightarrow \infty$, or for $M>1+\epsilon$, $s \rightarrow 1$ and r progresses from 0 to 1 so that

$$C_{X} \approx 2A(r)$$
.

Hence the polynomials A(r) and B(r) represent supersonic and subsonic parts of the drag curve respectively. Relatively few terms are needed; generally, linear or quadratic forms are adequate.

With regard to the constants K and L it is instructive to look at the value at M=K and the slope at that point. When M=K, r=0, s=0, and

$$C_{X} = a_{o} + b_{o}$$
,
 $K(dC_{X}/dM)|_{M=K} = a_{1} + b_{1} + (a_{o} - b_{o}) / L$.

Bearing in mind that $2a_0$ is the approximate value of C_X immediately above the transonic drag rise and $2b_0$ is the value immediately below it, then it follows that K is the value of Mach number when the drag is midway between these two levels. If L \ll 1, then 2L is the effective interval of Mach number over which the transonic drag rise, $2(a_0 - b_0)$ would be attained if the maximum slope were maintained throughout.

Finally, consider the asymptotic behaviour of the curve. Firstly, for subsonic incompressible flow, M 0, the axial force coefficient,

$$C_x = 2 \sum_{n=0}^{N_b} (-)^n b_n + 0 (M^2)$$

and secondly for hypersonic flow, M → ∞, axial force coefficient,

$$C_x = 2 \sum_{n=0}^{N_a} a_n + 0 (M^{-2}).$$

These are the correct asymptotic forms for the axial force coefficient at both ends of the Mach number range. The properties of the transonic drag rise and the asymptotic behaviour of the curve can be used to make initial estimates for the values of each parameter. The values can then be refined by parameter estimation or nonlinear least squares curve fitting methods.

APPENDIX II

CORIOLIS AND GRAVITY COMPONENTS

High accuracy is required in shell trajectory computation. The effects of Coriolis force and the changes to the gravity vector, occurring along the trajectory, have a significant effect on the trajectory. Therefore these changes must be included in the mathematical model. Both effects are well known and documented, but are included here so that the document is self-contained as far as the description of the mathematical model of the shell trajectory is concerned.

The Coriolis acceleration arises from the rotation of the range axes system, because the range axes system is fixed relative to a rotating earth. The acceleration vector, Λ in equation (2), is given by

$$\Lambda = 2 \Omega \times U$$

where U is the velocity of the shell and Ω is the angular velocity of the earth, 7.292115 x 10^{-5} rads/s about an axis from south pole to north pole. Then at latitude Θ , positive south, and line of fire bearing Ψ from true north

$$\begin{bmatrix} \Omega_1 \\ \Omega_2 \\ \Omega_3 \end{bmatrix} = \begin{bmatrix} 2\cos\Theta & \cos\Psi \\ 2\cos\Theta & \sin\Psi \\ 2\sin\Theta \end{bmatrix} | \Omega|$$

assuming that the OX axis is along the line of fire, the OZ axis vertically downwards and the OY axis horizontal to the right, thus forming a right handed axes system.

The second part of this appendix looks at the problem of defining the components of gravity in the same axes system. The magnitude of the acceleration due to gravity at a distance r from the centre of the earth is

$$|g| = g_0 r_0^2 / r^2$$

where g is the local acceleration at mean sea level and r_0 is the radius of the earth. The direction of the acceleration is radially inwards. Then at a point (x,y,z) in a Cartesian coordinate system with axes as described above and origin at an altitude, h_0 , above mean sea level the gravity vector can be represented by

$$g = -g_0 r_0^2 [x \dot{i} + y \dot{j} - (h_0 + r_0 - z) \dot{k}] / r^3$$

where $r^2 = x^2 + y^2 + (h_0 + r_0 - z)^2$. This result can be easily derived from the geometry of the situation, using the knowledge that x, y and z are all very small compared with r_0 .

APPENDIX 111

PARTIAL DERIVATIVES WITH RESPECT TO PARAMETERS FOR SHELTRAJ

In order to implement a parameter estimation algorithm we need to know partial derivatives of the measured variables with respect to the unknown parameters. These partial derivatives are obtained by numerical solution of a set of simultaneous ordinary differential equations obtained by partial differentiation of the mathematical model equations presented in Section 3.1. By separating out the components of velocity and acceleration in equation (2) and differentiating with respect to the parameter, P_i, we obtain the following set of differential equations

$$\frac{d^{2}}{dt^{2}}\left(\frac{\partial x}{\partial P_{i}}\right) = \left(\frac{\rho S}{2m}\right)\left(C_{D}V_{1}\frac{\partial V}{\partial P_{i}} + C_{D}\frac{\partial V_{1}}{\partial P_{i}}V_{1} + \frac{\partial C_{D}}{\partial P_{i}}V_{1}V\right) + \frac{\partial g_{1}}{\partial P_{i}} - \frac{\partial \Lambda_{1}}{\partial P_{i}}$$
(15)

$$\frac{d^{2}}{dt^{2}} \left(\frac{\partial y}{\partial P_{i}} \right) = \left(\frac{\rho S}{2m} \right) \left(C_{D} V_{2} \frac{\partial V}{\partial P_{i}} + C_{D} \frac{\partial V_{2}}{\partial P_{i}} V + \frac{\partial C_{D}}{\partial P_{i}} V_{2} V + 2C_{L} V \frac{\partial V}{\partial P_{i}} + \frac{\partial C_{L}}{\partial P_{i}} V^{2} \right) + \frac{\partial g_{2}}{\partial P_{i}} - \frac{\partial \Lambda_{2}}{\partial P_{i}}$$
(16)

$$\frac{d^{2}}{dt^{2}}\left(\frac{\partial z}{\partial P_{i}}\right) = \left(\frac{\rho S}{2m}\right)\left(C_{D}V_{3}\frac{\partial V}{\partial P_{i}} + C_{D}\frac{\partial V_{3}}{\partial P_{i}}V + \frac{\partial C_{D}}{\partial P_{i}}V_{3}V\right) + \frac{\partial g_{3}}{\partial P_{i}} - \frac{\partial \Lambda_{3}}{\partial P_{i}}$$
(17)

$$\frac{d}{dt}(\frac{\partial p_s}{\partial P_i}) = (\frac{\rho S d^2}{4I_x})(C_{\ell_p} p_s \frac{\partial V}{\partial P_i} + C_{\ell_p} \frac{\partial p_s}{\partial P_i} V + \frac{\partial C_{\ell_p}}{\partial P_i} p_s V)$$
(18)

if we assume that local air density, ρ and speed of sound a, are insensitive to changes in parameter values. These then are the basic differential equations which can be solved to provide values of the partial derivatives,

$$\frac{\partial_x}{\partial P_i} \frac{\partial y}{\partial P_i}$$
, $\frac{\partial z}{\partial P_i}$ and $\frac{\partial P_s}{\partial P_i}$

required by the parameter estimation algorithm. However, these equations include many partial derivatives which are not available from the solution of the equations but must be obtained by partial differentiation of other relationships. The method of calculating these partial derivatives is outlined below. Using the relation

$$V^2 = V_1^2 + V_2^2 + V_3^2 .$$

we find that

$$V \frac{\partial V}{\partial P_i} = V_1 \frac{d}{dt} (\frac{\partial x}{\partial P_i}) + V_2 \frac{d}{dt} (\frac{\partial y}{\partial P_i}) + V_3 \frac{d}{dt} (\frac{\partial z}{\partial P_i}) ,$$

since it follows easily from the relation between velocity relative to range axes and true air velocity that

$$\frac{\partial}{\partial P_{i}} \begin{bmatrix} V_{1} \\ V_{2} \\ V_{3} \end{bmatrix} = \frac{d}{dt} \left\{ \frac{\partial}{\partial P_{i}} \begin{bmatrix} x \\ y \\ z \end{bmatrix} \right\}.$$

Using the expressions given in Appendix II for the accelerations due to Coriolis and gravity effects, the following results can be derived;

$$\frac{\partial}{\partial P_{i}} \begin{bmatrix} \Lambda_{i} \\ \Lambda_{2} \\ \Lambda_{3} \end{bmatrix} = 2 \begin{bmatrix} \Omega_{1} \\ \Omega_{2} \\ \Omega_{3} \end{bmatrix} \frac{d}{dt} \left\{ \begin{array}{c} \partial \\ \partial P_{i} \\ z \end{array} \right\}$$

and

$$\frac{\partial}{\partial P_{i}} \begin{bmatrix} g_{1} \\ g_{2} \\ g_{3} \end{bmatrix} \approx -g (r_{0}/r)^{2} \frac{1}{r} \frac{\partial}{\partial P_{i}} \begin{bmatrix} x \\ y \\ z \end{bmatrix},$$

although the approximation in this equation is negligible. The partial derivatives of the aerodynamic force and moment coefficients can be obtained from equations (1), (3), (5), (6) and (7) which can be combined to define the coefficients in terms of the parameters, P_i . This yields the following results,

$$\frac{\partial C_{D}}{\partial P_{i}} = -\frac{\partial Cx}{\partial P_{i}} \cos \xi - \frac{\partial Cz}{\partial P_{i}} \sin \xi + C_{L} \frac{\partial \xi}{\partial P_{i}}$$

$$\frac{\partial C_L}{\partial P_i} = \frac{\partial C_X}{\partial P_i} \sin \zeta - \frac{\partial C_Z}{\partial P_i} \cos \zeta - C_D \frac{\partial \zeta}{\partial P_i}$$

From the expression for the yaw of repose it follows that

$$\frac{\partial \zeta_{R}}{\partial P_{i}} = (2I_{X}/\rho SdC_{m\zeta} V^{5}) \left\{ V_{P_{S}} V_{1} \frac{\partial g_{3}}{\partial P_{i}} + V_{P_{S}} \frac{\partial V_{1}}{\partial P_{i}} g_{3} + V_{N} \frac{\partial V_{N}}{\partial P_{i}} g_{3} + V_{N} \frac{\partial V_{$$

Finally, using the parametric representations of the aerodynamic coefficients, we obtain the results, for the axial force coefficient,

$$\frac{\partial C_{x}}{\partial P_{i}} = (1+s)(\delta_{9i} + \delta_{10i}r + \delta_{11i}r^{2}) + (1-s)(\delta_{12i} + \delta_{13i}r + \delta_{14i}r^{2})$$

$$+ (P_{q} + P_{10}r + P_{11}r^{2} - P_{12} - P_{13}r - P_{14}r^{2}) \frac{\partial s}{\partial P_{i}}$$

$$+ [(1+s)(P_{10} + 2P_{11}r) + (1-s)(P_{13} + 2P_{14}r)] \frac{\partial r}{\partial P_{i}}$$

where

$$\frac{\partial s}{\partial P_{i}} = [P_{8}^{2} \frac{\partial r}{\partial P_{i}} + r(r^{2}-1) P_{8} \delta_{8i}] [(1-P_{8}^{2}) r^{2} + P_{8}^{2}]^{-3/2},$$

$$\frac{\partial r}{\partial P_{i}} = [2MP_{7}^{2} \frac{\partial M}{\partial P_{i}} - 2M^{2}P_{7}\delta_{7i}] [M^{2} + P_{7}^{2}]^{-2}$$

and

$$\frac{\partial M}{\partial P_i} \approx \frac{1}{a} \frac{\partial V}{\partial P_i}$$

Similarly for the normal force coefficient, we obtain

$$\frac{\partial C_z}{\partial P_i} = \frac{\partial C_{z\xi}}{\partial P_i} + C_{z\xi} \frac{\partial \xi}{\partial P_i}$$

$$\frac{\partial c_{z\xi}}{\partial P_i} = (1+f)(\delta_{17i} + \delta_{18i}g^2) + (1-f)(\delta_{20i} + \delta_{21i}g + \delta_{22i}g^2)$$

$$+ (P_{17} + P_{18}g + P_{19}g^2 - P_{20} - P_{21}g - P_{22}g^2) \frac{\partial f}{\partial P_i}$$

$$+ [(1+f)(P_{18} + 2P_{19}g) + (1-f)(P_{21} + 2P_{22}g)] \frac{\partial g}{\partial P_i}$$

where

$$\frac{\partial f}{\partial P_{i}} = \left[P_{16}^{2} \frac{\partial g}{\partial P_{i}} + g(g^{2} - 1) P_{16}^{3} \delta_{16i} \right] \left[(1 - P_{16}^{2}) g^{2} + P_{16}^{2} \right]^{-3/2}$$

$$\frac{\partial f}{\partial P_{i}} = \left[2MP_{15}^{2} \frac{\partial M}{\partial P_{i}} - 2M^{2} P_{15}^{3} \delta_{15i} \right] \left[M^{2} + P_{15}^{2} \right]^{-2}$$

While the rolling moment coefficient representation yields the result,

$$\frac{\partial C_{\ell}}{\partial P_{i}} = (\delta_{23i} + \delta_{24i} M + \delta_{25i} M^{2} + \delta_{26i} M^{3}) + (P_{24} + 2P_{25}M + 3P_{26}M^{2}) \frac{\partial M}{\partial P_{i}}.$$

The equations in this appendix embody all the information necessary for calculating those partial derivatives required by the parameter estimation algorithm to estimate corrections for the initial estimates of the parameter values. If all 27 parameters are allowed to vary, the equations (15) to (18) represent 189 simultaneous, first order, ordinary, differential equations. So, including the equations (2), which define the mathematical model, we find that for each iteration of the parameter estimation algorithm 197 first order equations must be solved.

APPENDIX IV

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APPENDIX V

YAWSONDE CALIBRATION

Consider the yawsonde depicted in figure 4. It consists of two sun slits at angles γ_1 and γ_2 to the longitudinal axis of the shell as shown in figure 4(c). The centres of the slits are separated by rotation about the shell longitudinal axis through an angle β in figure 4(b). When the shell rotates during flight a train of pulses of opposite polarity like the train in figure 4(d) with period T, the roll period, is emitted by each sensor. The relationship connecting the time, τ , between pulses of opposite polarity and the complementary solar aspect angle, $\sigma_{\rm N}$ in figure 4(a), is the calibration curve of the yawsonde. This appendix is concerned with the derivation of that curve. It is assumed during the derivation that the shell does not pitch or yaw so that the direction of the longitudinal axis remains constant. The errors arising from this assumption

will not be significant if the roll rate is much greater than the nutation and

precession rates, as is generally the case.

If the sum is detected by sensor 1 of the yawsonde them it lies in the half plane defined by the relations,

$$x'' \sin \gamma_1 - y'' \cos \gamma_1 = 0, z'' > 0$$
 (19)

where the axes system Sx"y"z" is fixed in the shell and rotates with it; Sx" is forward along the shell axis, Sz" is outwards through the centre of sensor 1 and Sy" completes a right handed set as shown in figure 4. The sun is likewise detected by sensor 2 when it lies in the half plane defined by the relations

$$x'' \sin \gamma_2 - y'' \cos \gamma_2 \cos \beta - z'' \cos \gamma_2 \sin \beta = 0,$$

$$z'' \cos \beta - y'' \sin \beta \geqslant 0.$$
(20)

If the angular velocity component about the longitudinal axis is P_s , then

$$2\pi p_{S} = 1/T,$$

and the direction cosines of the sun in terms of the complementary solar aspect angle are

$$(\sin\sigma_N, \cos\sigma_N \sin\rho_s t, \cos\sigma_N \cos\rho_s t)$$
 (21)

where t is time measured from when the sun is in the Sx"z" plane. Hence using equations (19) to (21), the complementary solar aspect angle can be determined from the measured time interval, τ , by the relation

$$\tan \sigma_{N} = -\sin (2\pi\tau/T + \beta) / [\tan^{2}\gamma_{1} + \tan^{2}\gamma_{2} - 2\tan\gamma_{1} \tan\gamma_{2} \cos (2\pi\tau/T + \beta)]^{\frac{1}{2}}$$
 (22)

In order to obtain a symmetrical calibration curve and make optimum use of the yawsonde, the nominal values which are usually chosen for the parameters in equation (22) are $\gamma_1 = -\gamma_2 = \gamma_1$ where γ is generally between $\pi/6$ and $\pi/4$, and

 $\beta = \pi$. If we substitute into equation (22) for γ_1 , γ_2 and β we find that

$$\tan \sigma_{N} = \cos (\pi \tau / T) / \tan \gamma. \tag{23}$$

It follows from the expression (23), since $0 \le \tau \le T$, that the range of complementary solar aspect angles which can be measured by the yawsonde is

$$- (\pi/2 - \gamma) \leqslant \sigma_{N} \leqslant + (\pi/2 - \gamma). \tag{24}$$

Figure 5 shows a typical yawsonde calibration curve of the type described by equation (23) with $\gamma = \pi/4$. The curve is approximately linear over much of its range. The extremities of the curve are not of much interest since experiments will generally be designed to avoid this area for two reasons. Firstly pulses from the two sensors will tend to interfere and the experimental record will be difficult to decipher. Secondly, the finite dimensions of the sun slits, which have been ignored in deriving the calibration curve (22), will make the calibration invalid for values of τ/T approaching 0 or 1.

The slope of the curve at $\tau/T = 1/2$ will be a good measure of the overall sensitivity of the yawsonde, that is,

$$d\sigma_{N} |d(\tau/T)|_{\tau/T=1/2} = -\pi/\tan\gamma.$$

Clearly it is necessary to compromise when choosing a value of γ , the angle each slit makes with the longitudinal axis of the shell. If γ is much greater than $\pi/4$ the sensitivity given in this equation begins to fall away rapidly. However, the value of γ should be as large as possible to provide an adequate range of measurement as defined by relation (24), particularly since it is not practical to use the total range for τ , from 0 to T.

APPENDIX VI

LISTING OF PROGRAM YAWCAL

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APPENDIX VII

SOLAR ASPECT ANGLE

In order to use the data on the complementary solar aspect angle which is measured with the yawsonde one must know the position of the sun. The solution for the azimuth and elevation of the sun in range axes is given in reference 14, obtained using the method given in reference 15. The derivation uses the sidereal time, $(ST)_0$, corresponding to the Universal or Greenwich mean time at which the position of the sun is required. The sidereal time is the Hour Angle of the first point of Aries. The right ascension, RA, and the declination, δ , of the sun are also used. All three can be obtained from the Astronomical Ephemeris(ref.16) by interpolating between values given for each variable at 0 hours Universal Time, UT. Then, the local sidereal time.

LST =
$$(ST)_0 + \frac{366.2422}{365.2422}$$
 UT - Φ ,

where Φ is the longitude of the shell, and the hour angle of the sun,

$$H = LST - RA$$

so that the azimuth, $\boldsymbol{\psi}_{\mathrm{S}},$ and elevation, $\boldsymbol{\theta}_{\mathrm{S}},$ of the sun in earth axes are given by

$$\sin \theta_{s} = \sin \delta \sin \Theta + \cos \delta \cos \Theta \cos H$$

$$\cos \psi_{s} \cos \theta_{s} = \sin \delta \cos \Theta - \cos \delta \sin \Theta \cos H$$

$$\sin \psi_{s} \cos \theta_{s} = \sin H \cos \delta.$$

It must be remembered that the azimuth, $\psi_{\rm S}$, is measured relative to true north, so that if Ψ is the azimuth of the shell relative to true north, the complementary solar aspect angle is given by

$$\sin \sigma_{N} = \cos \theta_{s} \cos \psi_{s} \cos \theta \cos \Psi + \cos \theta_{s} \sin \psi_{s} \cos \theta \sin \Psi + \sin \theta_{s} \sin \theta$$

where θ is the angle of elevation of the shell. The angle Ψ has two components, Ψ_{o} , the bearing of the line of fire of the shell and ψ , the angle of azimuth of the shell relative to the line of fire, so that $\Psi=\Psi_{o}+\psi$. The above expression can be rearranged to give

$$\sin \sigma_{N} = \cos \theta_{S} \cos \theta \cos (\psi_{S} - \Psi) + \sin \theta \sin \theta_{S}$$
 (25)

so that the origin used to measure the angles of azimuth is no longer relevant and the most convenient origin can be used. The expression (25) is needed both for trials planning and data analysis. For trials planning purposes, it is generally convenient to refer both azimuth angles to true north because the bearing of the line of fire is used to approximate the azimuth of the shell. However, in analysing flight data it is more convenient to refer azimuth measurements to range axes. Details of how the expression (25) is used are given in Section 4.

APPENDIX VIII

LISTING OF PROGRAM ASPECT

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APPENDIX IX

PARTIAL DERIVATIVES WITH RESPECT TO PARAMETERS FOR YAWSONDE

The parameter estimation algorithm which is used to analyse the yawsonde data requires, as input, values of partial derivatives of the complementary solar aspect angle with respect to each of the parameters. These partial derivatives are obtained by partial differentiation of the expression (25) which defines the complementary solar aspect angle. Thus the partial derivatives are defined by the relation

$$\cos \sigma_{N} \frac{\partial \sigma_{N}}{\partial P_{i}} = -\left[\cos \theta_{s} \sin \theta \cos(\psi_{s} - \psi) + \sin \theta_{s} \cos \theta\right] \frac{\partial \theta}{\partial P_{i}} + \cos \theta_{s} \cos \theta \sin(\psi_{s} - \psi) \frac{\partial \psi}{\partial P_{i}}$$
(26)

The partial derivatives needed to evaluate equation (26) are obtained by numerical integration of a set of ordinary differential equations which are derived from the mathematical model equations (9) by partial differentiation. This results in the following equations being obtained

$$\frac{d}{dt} \left(\frac{\partial \psi}{\partial Pi} \right) = \frac{\partial r}{\partial Pi} \sec \theta + r \sec \theta \tan \theta \frac{\partial \theta}{\partial Pi} ,$$

$$\frac{d}{dt} \left(\frac{\partial \theta}{\partial Pi} \right) = \frac{\partial q}{\partial Pi}$$

$$\frac{d}{dt} \left(\frac{\partial q}{\partial Pi} \right) = \left[p - (I_{\chi}/I)p_{S} \right] \frac{\partial r}{\partial Pi} + r \frac{\partial p}{\partial Pi} + (\frac{QSd}{I}) \left[\left(\frac{\partial Cm}{\partial \zeta} \right) \cos \phi \right]$$

$$- \left(\frac{P_{S}d}{2V} \right) \frac{\partial Cnp}{\partial \delta} \sin \phi + \frac{\partial Cmq}{\partial \zeta} \left(\frac{qd}{2V} \right) \frac{\partial \zeta}{\partial Pi} - \left[C_{m} \sin \phi \right]$$

$$+ C_{mp} \left(\frac{P_{S}d}{2V} \right) \cos \phi \right] \frac{\partial \phi}{\partial Pi} + C_{mq} \left(\frac{d}{2V} \right) \frac{\partial q}{\partial Pi} + \frac{\partial Cm}{\partial Pi} \cos \phi$$

$$- \frac{\partial Cnp}{\partial Pi} \left(\frac{P_{S}d}{2V} \right) \sin \phi + \frac{\partial Cmq}{\partial Pi} \left(\frac{qd}{2V} \right) \right] ,$$

$$\frac{d}{dt} \left(\frac{\partial r}{\partial Pi} \right) = \left[-p + (I_{\chi}/I)p_{S} \right] \frac{\partial q}{\partial Pi} - q \frac{\partial p}{\partial Pi} + \left(\frac{QSd}{I} \right) \left[\frac{\partial^{C}m}{\partial \zeta} \sin \phi + \frac{\partial Cnp}{\partial \zeta} \left(\frac{P_{S}d}{2V} \right) \cos \phi + \frac{\partial Cmq}{\partial \zeta} \left(\frac{rd}{2V} \right) \right] \frac{\partial \zeta}{\partial Pi} + \left[C_{m} \cos \phi - Cnp \left(\frac{P_{S}d}{2V} \right) \sin \phi \right] \frac{\partial \phi}{\partial Pi} + Cmq \left(\frac{d}{2V} \right) \frac{\partial q}{\partial Pi}$$

$$+ \frac{\partial Cm}{\partial Pi} \sin \phi + \frac{\partial Cnp}{\partial Pi} \left(\frac{P_{S}d}{2V} \right) \cos \phi + \frac{\partial Cmq}{\partial Pi} \left(\frac{rd}{2V} \right) \right] .$$

By partial differentiation of equation (10) we obtain the relation

$$\frac{\partial \mathbf{p}}{\partial \mathbf{P}i} = -\frac{\partial \mathbf{r}}{\partial \mathbf{P}i} \tan \theta - \mathbf{r} \sec^2 \theta \frac{\partial \theta}{\partial \mathbf{P}i}$$

Using the parametric representations of the aerodynamic coefficients defined in equation (12) we can obtain the following relations by partial differentiation

$$\frac{\partial C_{m}}{\partial \zeta} = P_{5} + P_{12}M + 3P_{6} \zeta^{2} + 5P_{7} \zeta^{4} ,$$

$$\frac{\partial C_{np}}{\partial \zeta} = p_{8} + 3P_{9} \zeta^{2}$$

$$\frac{\partial C_{mq}}{\partial \zeta} = 2P_{11} \zeta ,$$

$$\frac{\partial C_{m}}{\partial P_{1}} = (\delta_{5i} + \delta_{12i} M) \zeta + \delta_{6i} \zeta^{3} + \delta_{7i} \zeta^{5} ,$$

$$\frac{\partial C_{np}}{\partial P_{1}} = \delta_{8i} \zeta + \delta_{9i} \zeta^{3} ,$$

$$\frac{\partial C_{mq}}{\partial P_{1}} = \delta_{10i} + \delta_{11i} \zeta^{2} .$$
(28)

Finally the partial derivatives of the magnitude and the orientation of the incidence can be obtained from the definitions given in equations (13) and (14), so that

$$\frac{\partial \xi}{\partial P_{i}} = u \left(v \frac{\partial v}{\partial P_{i}} + w \frac{\partial w}{\partial P_{i}} \right) / V^{2} \left(v^{2} + w^{2} \right)^{\frac{1}{2}} - \left(v^{2} + w^{2} \right)^{\frac{1}{2}} \frac{\partial u}{\partial P_{i}} / V^{2}$$

$$\frac{\partial \phi}{\partial P_{i}} = \left(v \frac{\partial w}{\partial P_{i}} - w \frac{\partial v}{\partial P_{i}} \right) / \left(v + w^{2} \right)$$
(29)

where

$$\frac{\partial u}{\partial P_{1}} = -w \frac{\partial \theta}{\partial P_{1}} + v \cos \theta \frac{\partial \psi}{\partial P_{1}}$$

$$\frac{\partial v}{\partial P_{1}} = -(V_{1} \cos \psi + V_{2} \sin \psi) \frac{\partial \psi}{\partial P_{1}}$$

$$\frac{\partial w}{\partial P_{1}} = u \frac{\partial \theta}{\partial P_{1}} + v \sin \theta \frac{\partial \psi}{\partial P_{1}}$$

The relations (28) and (29) can be used to evaluate the terms in the differential equations (27). It then becomes possible to integrate the differential equations numerically and so find the values of the partial derivatives needed to evaluate the equations (26).

APPENDIX X

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\$1644411.570796-DARCOS(COSSIG)	000000	U	
	0000000	U	FDS=1.00-15
SECSHII - / DCOS (SIGNAN)	00000000		CALL SINV(PSI,NP,EPS, IER)
	0.000000		#PITE (6.1) 1EA
TAC JORDER (1) . GT . NOARAW) GO TO 150	0000000		STOP
CORDERON CONTRACTOR CO	04400000	0 0	
oC05746 ev(401+2))	0000000		ESTIMATE CORRECTIONS AND PROBABLE ERRORS
	000000000000000000000000000000000000000	100	00 110 1=1.NP
DUTOUT RESULTS OF INTEGRATION STEP IF REDUIRED	0000000		0 8 0 7
The state of the s	000000000000000000000000000000000000000		00 130 1=1-MP
# (-(00000720		IF(14.F0.0) GO TO 125
	060000130	U	
ARTUAN.	000000740		KD=KD+1
	000000		
		120	Y () HF () + PSI (X D) + C & D (I)
	0100000		E(1)=E(1)+PSI(KD)+CWD(1)
SCHOOL THE SINCE STACES THE	00000015		PROPABLE ERRORS - FIRST CORRECTED VALUE OF STANDARD DEVIATION
ADUTINE FROM SYSTEM/300 SCIENTIFIC SURROUTINE PACKAGE	0000000		
INVESTING A DOSITIVE DEFINITE SYMBETRIC MATRIX	0000000	-	O STORMEST CHA-F(I) F(WO) I)
CALL WFSD (A.N.EPS.IER)	04000000		SIGMA=DSORT(SIGWA/DIV)
INCIEDALTON METURN	00000000		00 150 1=1.00
	06000000	150	
	0010000	U	
(>1a1 - 000) 1 1 1 1 1 1 1 1 1	0210000	U	SIGSONS IGNAS IGNA
	000000130		DO 160 I=1.KD
	000000	180	0 PSI(1) = PSI(1) • SI650
IF (KEND-LE-0) GO TO 500	000000		
	59100000		I FORWATE DOUBTFUL WHETHER MATRIX FOR INVENSION IS POSITIVE DEFINITIONOUSSION

TABLE 1. TYPICAL AERODYNAMIC DATA FOR A SHELL

М	c _x	Cyp5	Czţ	C p	C _m ç	C _{np} ç	C _{mq}
0.0	-0.1299	-1.5	-1.7851	-0.0357	3.5730	0.0	-12.0
0.5	-0.1299	-1.5	-1.7851	-0.0290	3.6756	0.0	-13.0
0.55	-0.1299	-1.5	-1.7851	-0.0284	3.6931	0.0	-13.0
0.60	-0.1299	-1.5	-1.7851	-0.0279	3.7222	0.0	-13.0
0.70	-0.1281	-1.5	-1.7831	-0.0270	3.7946	0.012	-15.0
0.75	-0.1250	-1.5	-1.7738	-0.0265	3.8330	0.025	-17.0
0.80	-0.1225	-1.5	-1.7563	-0.0261	3.8762	0.038	-18.0
0.825	-0.1217	-1.5	-1.7449	-0.0259	3.9018	0.044	÷19.0
0.850	-0.1214	-1.5	-1.7319	-0.0257	3.9318	0.05	-20.0
0.875	-0.1249	-1.5	-1.7206	-0.0255	3.9678	0.4	-21.0
0.90	-0.1338	-1.5	-1.7126	-0.0253	4.0124	0.75	-23.0
0.925	-0.1533	-1.5	-1.7172	-0.0252	4.0876	1.1	-24.0
0.94	-0.1769	-1.5	-1.7348	-0.0250	4.1697	1.1	-25.0
0.95	-0.1998	-1.5	-1.7551	-0.0250	4.2338	1.1	-25.0
0.96	-0.2266	-1.5	-1.7804	-0.0249	4.2916	1.05	-25.0
0.97	-0.2555	-1.5	-1.8090	-0.0248	4.3258	1.0	-24.0
0.98	-0.2849	-1.5	-1.8392	-0.0248	4.3161	0.94	-23.0
0.99	-0.3132	-1.5	-1.8695	-0.0247	4.2807	0.89	-23.0
1.00	-0.3391	-1.5	-1.8986	-0.0246	4.2341	0.85	-22.0
1.01	-0.3612	-1.5	-1.9250	-0.0245	4.1862	0.79	-21.0
1.02	-0.3784	-1.5	-1.9477	-0.0245	4.1415	0.75	-21.0
1.03	-0.3892	-1.5	-1.9651	-0.0244	4.1066	0.77	-21.0
1.04	-0.3958	-1.5	-1.9794	-0.0243	4.0749	0.65	-20.0
1.05	-0.4008	-1.5	-1.9932	-0.0243	4.0454	0.60	-20.0
1.075	-0.4085	-1.5	-2.0271	-0.0241	3.9922	0.52	-19.0
1.1	-0.4118	-1.5	-2.0620	-0.0239	3.9579	0.44	-18.0
1.125	-0.4124	-1.5	-2.0964	-0.0238	3.9369	0.37	-17.0
1.15	-0.4102	-1.5	-2.1281	-0.0236	3.9246	0.30	-16.0
1.20	-0.4007	-1.5	-2.1863	-0.0233	3.9120	0.20	-16.0
1.25	-0.3921	-1.5	-2.2422	-0.0230	3.9019	0.17	-15.0
1.30	-0.3839	-1.5	-2.3000	-0.0227	3.8920	0.13	-15.0
1.40	-0.3693	-1.5	-2.4061	-0.6221	3.8730	0.07	-14.0
1.50	-0.3566	-1.5	-2.5042	-0.0215	3.8342	0.0	-13.0
1.75	-0.3309	-1.5	-2.7107	-0.0203	3.7560	0.0	-13.0
2.00	-0.3104	-1.5	-2.8569	-0.0192	3.7232	0.0	-13.0
2.25	-0.2941	-1.5	-2.9393	-0.0182	3.6785	0.0	-13.0
2.50	-0.2841	-1.5	-2.9579	-0.0173	3.5650	0.0	-13.0

d = 0.105 S = 0.008659 m = 14.9688 moment reference = 0.3115 $I_X = 0.02326$ I = 0.22557

TABLE 2. FITTING ANALYTIC CURVES TO THE AXIAL FORCE COEFFICIENT

(a) NR3634

K	L	a _o	a ₁	a ₂	b _o	b ₁	r.m.s.
0.97956	0.04979	-0.22346	0.10800	-	-0.05871	-	0.00484
0.97719	0.05633	-0.22897	0.12629	-	-0.04734	0.04665	0.00165
0.97719	0.05634	-0.22899	0.12635	-0.00005	-0.04734	0.04666	0.00167

(b) Gavre

a	b	С	d	e	f	r.m.s.
-0.26447	0.09913	0.97206	19.963	-7.5430	-30.023	0.00903

NOTE: The Mach number range used in the nonlinear least squares fitting was 0.65 to 1.4

TABLE 3. ANALYTIC REPRESENTATIONS FOR OTHER COEFFICIENTS

(a) Normal force derivative

K	L	a _o	a ₁	a ₂	b _o	b ₁	r.m.s.
0.97321	0.02156	-0.94111	-0.74737	-	-0.87307	-	0.0180
0.96413	0.03441	-0.93980	-0.73030	-	-0.85000	0.13116	0.0060
0.96564	0.03584	-0.94492	-0.68620	-0.10380	-0.84917	0.13321	0.0059

(b) Roll damping derivative

a _o	a ₁	a ₂	a3	a ₄	r.m.s.
-0.03149	0.00648	-	-	-,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	0.000891
-0.03485	0.01251	-0.002279	-	-	0.000243
-0.03559	0.01569	-0.005577	0.000899	-	0.000068
-0.03570	0.01702	-0.008138	0.002558	-0.000339	0.000034

TABLE 4. DESCRIPTION OF CARD INPUT TO SHELTRAJ

Card	Format	Variable	Comments
1	20A4	TITLE (20)	A title card to describe the job being processed, reproduced on the output.
2	1615	LENTER	This variable controls a facility which allows the user to begin entering data at any one of several different points in the input routine.
			LENTER CARD
			1 3
			2 5
			3 15
			4 9
			5 13
			6 17
			7 18 8 20
			9 return
3	8F10.0	AMASS	Shell mass (kg)
		ROLLI	Moment of inertia about the longitudinal axis (kg m ²
		REFS	Reference area (m ²)
		BODIAM	Reference length (m)
4	8F10.0	OMEGA	Angular velocity of the earth. Since this is added
			to acceleration components by the program instead of
			subtracted from them, as in equation (2) a negative
			value should be entered.
			(-7.292115.10 ⁻⁵ rad/s)
		ALAT	Latitude of the shell, positive south (degrees)
		BEAR	Bearing of the line of fire relative to true north
		GRAV	(degrees) Acceleration due to gravity (ms ⁻²)
		HTASLO	Height of range origin above mean sea-level (m)
		RO	Radius of the earth (m)
5-8	8F10.0	XE (27)	The maximum changes allowed in each parameter, when testing for convergence.
9-12	8F10.0	X(27)	Initial estimates for values of the parameters Pi.
13-14	1615	JORDER (27)	Order of the parameters for internal use by the program particularly when determining the first NPARAM parameters.
15	8F10.0	то	Time at which integration begins.
16	8F10.0	XS(4)	Weighting factors proportional to the emphasis to be placed on each of the four measured quantities, range, deviation, altitude and roll rate.
17	8F10.0	REJECT ACCFAC	Initial data rejection level. Scaling factor multiplying all XE. Can be used for
		HMAX	wholesale adjustment of levels for convergence. Maximum value allowed for integration step size.
			This value will be used unless time to reach next data point is smaller.

TABLE 4 (CONTD.).

Card	Format	Variable	Comments
18 1615		NPARAM ITERN NPLOT	The first NPARAM parameters only, as specified in the JORDER array, will be allowed to vary. Maximum number of iterations of parameter estimation algorithm Plot every NPLOT th point of the simulated variable values. A maximum of 200 points can be plotted.
19	1615	LENTER LCASE IFOUT	A repeat of the options allowed by card 2. Principally to avoid inputting new experimental data if none is needed. Non-zero if data for another run follows. Non-zero if a record of the experimental data points is required.
20	1615	NPTS ISKIP	Number of data points to be used in this run. Use only every ISKIP point from the dataset containing the experimental measurements.
21	1615	IND	Control variable, describing the nature of the meteorological data, which is available = 1 none available = 2 wind table only = 3 pressure and temperature table only = 4 both wind table and pressure temperature table
		NWD	Number of points in wind tabulation
		NPT IFOUT	Number of points in tabulation of temperature and pressure Non-zero if meteorological data should be tabulated as it is read.

TABLE 5. SAMPLE INPUT DECK FOR SHELTRAJ

(a) Forces

14.968A		2326	0.	008659	0.	105							
7.2722F-0				5.		807	0.		637336	A	.01	0.001	
1.	1.		1.		1.	005	0.00		0.001		.01	0.001	
0.005	0.00			001	0.		0.01		0.01		.0001	0.0001	
0.00005		0001	1.										
0.	0.		0.			9.40	0.		-363.7	1 0	.9771A7	0.0563	
-0.22A973	0.1						240.04			0	.964132	0.0344	
-0.939A07	-0.	73030	3 0.		-0	. H4 99	0.13	1162	0.	-	0.03554	420.0156	919
-0.005577	120.0	12	7		9	,			4 18	2	5	19 15	22
		20	14	17	21	23	24 25	5 2					
0.													
1.	1.		1.		0.								
10.	1 .		0.	2									
2	6	0											
200	1	C											
1													
A TEST FO	FRCI	SF FF	1 TH	F ANAL	Y515	OF R	ADAR DA	TA FR	OM SHEL	L TRA	JECTOR I	ES - A	
7													
.3	6	C											
9	1	0							CHELL	TDA 15	CTORIES	- R	
TEST EXE	RCISE	FOR	THE	ANALY	515 0	F HAD	AH DAIA	r settim	SHELL	14.30	C turites		
,		0											
9	1	0											
TEST FEE	REISE	FOR	THE	ANALY	515 0	F RAD	AR DATA	FROM	SHELL	TRAJE	CTORIFS	- (
7													
•		0											
9	1	c				E 040		FROM	SHELL	TO 4 IF	CTORIES	- 0	
TEST EXE	PC 1 SF	FOR	THE	ANALY	515 (r HA							
		0											
9	1	C											
	RCISE	FOR	THE	ANALY	515	F RAD	AR DATA	FROM	SHELL	TRAJE	CTORIES	- 6	
7													
7	1	0											
	RCISE	FOR	THE	ANALY	SIS	F RAD	AR DATA	FROM	SHELL	TRAJE	CTORIES	- F	
7													
A	6	0											
0	1	0										- 6	
TEST FEE	DETER	FOR	THE	ANALY	SIS	E RAD	AR DATA	FDO	SHILL	TRAJE	CIORIES		
0		0											
	1	C											
TEST FEE	26 155	FOR	THE	AMALY	515	F RAP	AR DATA	FROM	SHELL	TRAJE	CTORLES	- H	
7													
10		0											
9	1	C											
	PCISE	FOR	THE	ANALY	515	F RAC	AR DATA	FRO	SHELL	TRAJE	CIORIES	- 1	
7													
11		0											
TEST EXE	00156		THE	ANALY	515	E PAT	AR DATA	FROM	M SHELL	TRAJE	ECTORIES	- 1	
7	46,36												
1.2	6	0											
9	1	0											
TEST EXE	PCISE	FOR	THE	ANALY	515	F RAT	AR PATA	FRC	SHELL	TRAJE	ECTORIES		
7		-											
13	6	0											
TEST EXE													
7													
14	6	C											
o	1	C											
TEST EXE	BC 15	- M											
7													
15		0											
TEST EXE													
7													
16	6	C											
9	1	0											
TEST EXE	RC15	- 0											
.,													
17	6	e											
4		6											

TABLE 5. SAMPLE INPUT DECK FOR SHELTRAJ

(b)	Rolling	moments

A DEC	K TO	TEST T	HE RO	LL FIT	TING	CAPAR	RILIT	IES OF	THI	S PROC	RAM				
14.96	AA .	0.0232	6 0	. COH65	9 0	.105									
7.2722				15.		. HO 7	0		•	373366					
1.		1.	1		1		1		1			. 1	0	.005	
0.02		0.01	0	.0001		.005		.005		.0001		. 1		.002	
0.1		0.05	C	.0001	0	.05	0	.01		.0001		.005		.001	
0.000	5	0.0001	1												
1.27		0.	1	· C ?	2	H9.	0		-	364.	0	.9768	c	.05731	
-0.229	96	0.12H9	0			0.0444	4 0	.06547	0			. 9641		.03441	
-0.916	52	-0.730	3 0		-	C.8307	. 0	.1312	0		-	0.036	0	.016	
0.		0.	1	390 .											
6	7	8	0	10	11	12	13	14	15	16	17	1 8	19	20	21
5.5	23	24	25	26	27	1	5	4	5	3					
0.															
0.			0		1										
10.			0	. 2											
1	50	0													
A	1	C													
200	1														
1															
ROLL 7	FSTI	4G - 6	•												
2	20	0													
9	1	0													
PULL	TEST	ING -	5R												
7															
3	20	0													
0		0													
	FSTI	46 - 6	C												
7															
4	20	c													
9	1	0													
ROLL 7	TEST	ING -	50												
5	20	2													
9	0	0													

TABLE 6. SIMULATED EXPERIMENTAL DATA FOR SHELTRAJ

Time	Range	Drift	Altitude	Roll rate
0.00C0CCOF+CO	2.8851295E+01	3.5840267E-04	-3-6210655E+0	1.3899733F+03
2.0000000F-01	5.7525682E+01	2.4925130E-03	-7.2103222F+01	1.38638636+03
3.0000COOF-C1	1.1435735F+02	7.552M3M2F-03 1.4637133F-02	-1.0768065F+02	1.38461916+03
4.0000000E-01	1.42519C3F+02	2.2687447E-U2	-1.7790246F+02	1.3811360F+G3
6.0000C00E-01	1.7051333E+02 1.9834287E+02	3.2380756E-02	-2.1255476E+02	1.3794197F+03
7.000000CF-01	2.2601057E+02	5.0258958E-02	-2.4095763E+02	1.3760365F+03
9.000G00GF-C1	2.5351827F+02 2.8086729F+02	7.5030253F-02 9.20F8361F-02	-3.1471407E+02	1.3743692E+03 1.3727178E+03
1.0000CCOF+00	3.0AC5951F+02	1.11207294-61	-3.#135424E+02	1.3710820E+03
1.2000000=+00	3.3509750F+02	1.32917056-61	-4.1424352F+02	1.3694619F+03
1.3000COF+CO	3.871907F+02	1.ACPAGAPE-01	-4.791739FF+02	1.36626705+03
1.500000000000	4.1536551F+02	2.0692057F-01 2.3505840F-01	-5.1122149E+02	1.36469205+03
1.6000000F+00	4.6803894F+02	2.4540128F-01	-5.7449465E+02	1.36156605+03
1.4000000F+00	4.9419014F+02 5.2019982E+02	3.3085925F-01	-6.0572510F+02	1.36005475+03
2.00000000000000	5.4606929F+02	3.4563329E-01	-A.673#742E+02	1.35703425+03
2.1000000F+00	5.7180011E+02	4.0222044F-01	-6.9782465E+02	1.3555447E+03 1.3540689E+03
2.1000C00F+C0	6.2285325E+02	4 . A1432A3F - 01	-7.5792264E+02	1.3526066F+03
2.4000000F+00	6.4H17A97F+02	5.2347995E-01	-7.4758743E+02	1.3511576F+03 1.3497214F+03
2.4000600F +CO	6.9H4357HE+02	6-1171614F-01	-8.4616375E+02	1.34829745+03
2.7000000F+00	7.2337006F+02 7.4F17741F+02	7.0688520F-01	-A.7507947E+02	1.3454850F+03
2.900CC0GF+C0	7.7285977E+02	7.5719923E-01	-9.3217852E+02	1.344007RE+03
3.000000CF+00	7.974190AE+02	A.0904335F-01 A.6226391F-01	-9.6036693E+02 -9.8831821F+02	1.3427238F+03
3.2000000F+00	8.4617524F+02	9.1690524E-01	-1.0160351E+03	1.34001375+63
3.4000000F+00	A.7037572F+02	9.73140A9F-01	-1.0435204F+03	1.3386756E+03
3.5000000F+00	9.1843143E+02	1.090F33AF+CG	-1.0978063F+03	1.3360317F+03
3.6000G00F+00	9.4729075F+02 9.6604050F+02	1.1521740E+00 1.2149849E+00	-1.1246122E+03	1.3347257F+03 1.3334307F+03
1.4000000E+00	9.8968265E+02	1 . 2 791 A99E +00	-1.1775638E+03	1.3321449F+03
4.000C000F+C0	1.0132191E+03	1.344 #24 3F+00	-1.2037151E+03	1.3306767E+03
4.1000000F+00	1.0599837E+03	1.4807879F+U0	-1.2553830E+03	1.32A3573F+03 1.3271147F+03
4.300C000F+00	1.0832166E+03 1.1063535E+03	1.55122816+00	-1.2409056E+03	1.325#811#+03
4.4000000F+00	1.12939736+03	1.49477836+00	-1.3313444E+03	1.3246577F+03 1.3234456F+03
4.6000COOF +00	1.1752197E+03	1 . 84 81 14 8E +00	-1.3810018E+03	1.3222427F+03
4.7000000E+00	1 - 198065 RE + 03 1 - 2207136E + 03	1.9259772E+00 2.0053908E+00	-1.4055486E+03	1.3210480F+03 1.3198613F+03
4.9000000F+0C	1.2433473F+03	2.0864052F+0C	-1.4541015E+03	1.21866256+03
5.0000000F+GC	1.24501000+03	2.1690262F.00 2.2532216E.00	-1.4781166E+03	1.3175114F+03
5.2000000F+00	1.3108427E+03	2.3389487E+00	-1.5256461E+03	1.3151940F+03
5.4000000F+00	1.33321826+03	2.42618345+00	-1.5491687E+03	1.31404916+03
5.5000000F+00	1.3778050E+03	2.6052513E+00 2.6971834E+00	-1.59574A7E+03	1.3117814F+03 1.3106577E+03
5.7000000F+00	1.4221930E+03	2.7907828E+00	-1 -6417312E+03	1.3095406F+03
5.8000000E+00	1.4443192E+03	2.8860787E+00 2.9830790E+00	-1.6645059E+03	1.30543015+63
6.0000000F+C0	1.4884480E+03	3.0817794E+C0	-1.7096353E+03	1.3062318F+03
6.2000000F+00	1.5104546E+03	3.1821762E +00 3.2842759E+00	-1.7319944F+03 -1.7542193F+03	1.30514415+03
6.3000000E+00	1.5543505F+03	3.3880 984F+00	-1.7763113E+03	1.3029860F+03
6.4000000F+00	1.5762624F+03	3.4936752E+66	-1.7982720E+03	1.30191516+03
6.600C000F+00	1.6199706E+03	3.7102299E+00	-1.8418050F+03	1.2997H9HF+03
6.7000000F+00	1.64177896+03	3.93415796+00	-1.8848275F+03	1.29766945+03
7.0000000F+00	1.64530756+03	4.0489215F+00 4.165558#F+00	-1.9061494F+03 -1.9273461E+03	1.29564865+03
7.1000000 +00	1.72A7231E+03	4.2840744F+00	-1 . 94 H4 1 H 3F +03	1.294585 AF+03
7.2000600F+00	1.7503901F+03 1.772030AE+03	4.4044754F+CC	-1.9901923E+03	1.29356356+03
7.4000CGOF+CO	1 . 7936457E+03	4.65099275+00	-2.010895AF +63	1.29153695+03
7.5000000F+00	1.8152354E+03	4.7771471F+00	-2.6314771E+03 -2.0519373F+03	1.2905321F+03 1.2895325E+03
7.700000F+00	1.8583402E+03	5.0353534E+U0	-2.0722768E+03	1.28853846+03
7.800G000F+00	1.0798561E+03	5.1674416E+C0 5.3015370E+00	-2.0924958F+03	1.2875494F+03
A.1000000F+00	1.9228165E+03	5.4376479E+00	-2.1325745E+03	1 • 2855872F • 03
A.2000000E+00	1.9442617F+03	5.5757804E+00 5.7159406E+00	-2.1524350E+03	1.2846138F+03
#.3000000E+00	1.9670837E+03 2.6084616E+03	5.85#1364E+00	-2.1918001E+03	1.28268236+03
A.5000000F+00	2.029A162F+03	6.1486793E+00	-2.230A933E+03	1.2807707E+03
A.6000COOF +GO	2.0511495E+03 2.0724610E+03	A.4475247F+G0	-2.2499637E+63	1+2798222F+03 1+2788787E+03
#.#000000E+00	2.0937510E+03	6.6001039F+00	-2.2001533F+03	1.27794005+03
9.0000000F+60	2.1150196E+03	6.754 RU 94E +00	-2.3070732F+03	1.27700605+63
9.1000000F+00	2.1574935F+03	7.0706528E+00	-2.344564 3E+03	1.27515246+03
9.2000000E+00	2.17#6992E+03 2.199##43E+03	7.2318120F+G0 7.3951408E+00	-2.3631361E+03	1.27423265+03
9.4000000F+00	2.2210489E+03 2.2421932E+03	7.5606455E+00 7.7283310E+00	-2.3999333E+03	1.272406AE+03
9.A00C0C0E+CO	2.26331726+03	7.8982020E+00	-2.4362700E+63	1.27059936+03
9.700000F+00	2.2844211E+03 2.3655649E+03	A.0702643E+00	-2.4542662F+03	1.26970236+03
9.9000000F+00	2.3245688E+03	#.4209951E+00	-2.4899151F+03	1.24792165+63
1.0000000F+01	2.3476129F+03 2.3686373E+03	# . 599AR54F + 00	-2.5075683E+03	1.26703785+03
1.020C000F+C1	2.3896420F+03 2.4106273E+03	9.1492211F+00	-2.5425331F+03	1.26528335+03
1.0400000F+C1	2.43159316+03	9.33693576+00	-2.57704356+03	1.2635459F+03
1.05000000 +01	2.4525397E+03	9.71924425.00	-2.59412ARE+03	1.2626835F+03

Time	Range	Drift	Altitude	Roll rate
1.070CC00F+01	2.49437526+03	9.91385756+00	-2.6279605F+03	1.26097135.03
1.0800000E+01	2.5152644F+03 2.5361346F+03	1.01107876+01	-2.6447072E+03	1.25927565+03
1 - 1 000 COOF + 01	2.5569861E+03	1.05116245+61	-2.6613413E+03	1.25842386+03
1.1100000F+01	2.5778187E+03	1.07155448+01	-2.6942726F+03	1.25759616+07
1.1300000F+01	2.5986328E+03 2.6194282E+03	1.0921809E+01	-2.7105701E+03	1.2567623F+03
1 - 1 4 00 00 0F + 01	2.6402C52E+03	1 - 1 34141 3F + 01	-2.7428297E+03	1.25510665+03
1.1500000F+C1	2.6609637E+03	1.1554775F+01	-2.7587921F+/3	1.2542846F+03
1.17CCCCCF+01	2.7024259F+03	1.19886815+01	-2.7746431F+03	1.25346656+03
1 . 1 #00000E +01	2.7231297E+03	1.22092516+01	-2.8060116F+63	1.25184176+03
1.1900000F+C1	2.7438154F+03 2.7644831F+03	1.24322506+01	-2.8215293F+03 -2.8369363F+03	1.25103506+03
1.510000000.01	2.7851329E+03	1.288558CF+01	-2.4522326E+C3	1.2494 TPRF +03
1.2200000F+01	2.805764HE+03 2.8263790E+03	1.3115932F+01	-2.8674185F+03	1.24863726+03
1.2400000F+01	2.8469754E+03	1.35840545+01	-2.8974543F+03	1.2476453F +03
1.2500000E+01	2.8675543E+03	1.3821841F+01	-2.4123145E+03	1.24627245+01
1.2600000E+01	2.88H1156F+03	1.43049045+01	-2.9270599E+03	1.24549126.03
1.2800000F+01	2.9291858E+03	1.4550201F+G1	-2.95622146+03	1.24393956+63
1.2900000F+C1	2.9496949E+03	1.47980196+01	-2.9706379E +03	1.24316916.63
1.3000000F+01	2.9701A6HE+03 2.9906614E+03	1.5048368E+61	-2.9949450F+03	1.24240205+03
1 . 3200000F + 61	3.01111906+03	1.55567116+01	-3.0132319E+33	1.24087805.04
1.3300000F+01	3.03155956+03	1.58147305+01	-3.6272119F+03	1.23936766.03
1.3500000F+C1	3.0773896F+03	1.63385256+01	-3.0548456E+03	1.23861736+03
1.3600000E+01	3.0927794E+03	1.66043265+01	-3.CAR4997F+03	1 . 237876 35 +63
1.3700000F+01	3.1131524F+03 3.1335087F+03	1.6872746F+01 1.7143796F+01	-3.0820454F+03	1.23712646+03
1.3900000F+C1	3.1538484E+03	1.74174855.01	-3.1088121F+03	1.23564795.03
1 .4 000000F +01	3.1741715E+03	1.7693825E+01	-3.12203346.03	1.23491326.63
1.4100000F+01	3.19447A1F+03	1.79728246+01	-3.1351468F+03	1.23418176.03
1.4300C00F+G1	3.2350420F+03	1.8538835F+01	-3.1610505F +03	1.23272765+03
1.4400G00F+01	3.2552994E+03 3.27554C6E+03	1.9825865E+01	-3.173841CF+33	1.23200510.63
1.4600000F+01	3.2957655E+03	1.94080195+01	-3.1991001F+03	1.2305688F.03
1.4700000F+61	3.31597446+03	1.9763163F+01	-3.2115689E+G3	1.72985505.03
1.4900000F+01	3.3561671F+03	2.0001030F+01 2.0301632F+01	-3.2239307F+03	1.22914426+63
1.5000000F+01	3.3765046F+03	2.06C4980E+01	-3.24R333RF+03	1.22773105+03
1.510C00CF+61	3.3966494F+03	2.0911086F+01	-3.26C3753E+C3	1.22702865.03
1.5200000E+01	3.4368917E+03	2.1219961F+01 2.1531617F+01	-3.2723103F +03 -3.2841388F +03	1.22532916.03
1 . 5 4 00 0 0 0 F + 0 1	3.456GH91E+03	2 - 1 8460676+61	-3.2958611F+63	1.22493925+03
1.550G00CF+C1	3.4776710F+03	2.216.1323F+01 2.24F3396=+01	-3.30747736+03 -3.3189#736+03	1.223558 0 -03
1.5700C00F+01	3.5171H7HF+03	2 . 280629RF + 61	-3.3303915E+63	1.22287236.03
1.5400000F+01	3.5372229E+03	2.313204CF+01	-X.2416898 +0 t	1.22218901.01
1.590CC0CF+01	3.5572425F+03	2.3460634F+C1 2.3792090F+C1	-3.1528823F+03	1.22053046+03
1.41000000 +01	3.5972357F+03	2.4126418F+01	-1.174 950RF +0.3	1.22015500.03
1.63000000001	1.61720946 +01	2.4463628F+01	-1. WERPAGE +0.1	1.21948245.61
1.64000000 +01	1.6" 711111 +01	2.51467311 +01	-1.407.4.141.01	1.21914496464
1.60000000001	3.67/03027+03	2.5492644F +01 2.5841478F +01	~1.417824GF+03	1.21748011 +03
1.A700000F+01	3.7168504F+03	2.61932415 +01	-1.4 186 305F +03	1.21661706.01
1.6800000F+01	3.73673356+03	2.4547944F+01	-3.44RR766E+03	1.21550000 +03
1.6900C00F+G1	3.7566017E+03	2.6905597E+C1 2.7266210E+01	-3.45901MCF+03	1.21484521 +03
1 . 7100GOOF +01	3.79629376 +03	2.76297946 +01	-3.47P9876F+03	1.21354425.03
1.7200000F+01	3.4161175E+03	2.79963600+01	-3.4RRR15RE+03	1.21289696+03
1.7400000E+C1	3.8557212F+03	2.8365919F+01 2.8738482E+01	-3.4985399E+03	1.21225196.03
1 - 75000000 +01	3.8755011F+63	2.9114061E+01	-3.517675HE +03	1.21096925.03
1.7600000F+01	3.8952665E+03	2.9492665E+01 2.9874308F+01	-3.5270A79E+03	1.21033135.03
1 . 78000G0F + C1	3.934753AE+03	3.0259COCE+01	-3.5456008F+03	1.20906256+03
1.79000000 +01	3.95447596+03	1.0646752E+01	-3.554701PF+03	1.2094715F+03
1.#100G00F+01	3.9741836E+03	3.1037575E + 01 3.1431479E + 01	-3.5636993F+63 -3.5725535F+03	1.20760265+03
1.#200000F+61	4.0135562F+03	3.1828476F+01	-3.581 386 3F+03	1.2055205+63
1.84000000 +01	4.6332212E+03	3.2228576E+01	-3.59C0720F+03	1.20592995.03
1 . A . 000000E +01	4.0725087E+03	3.3038123F +01	-3.5986565E+C3	1.20530995.63
1.8600C00E+01	4.09213146+03	3.34475916+01	-3.61551678+03	1 - 20407545 + 63
1 . # 700000F + 01	4.1117401E+03	3.38602026+01	-3.62379256.03	1.2034628F+03
1 . #900000E +01	4.1509156E+03	3.4694RA9E+01	-3.6400360F+03	1.2027418E+03
1.900000000001	4 . 1 704 A25F +03	3.5116986E+01	-3.6480039E+03	1.20163435+03
1.92000000001	4.1900356E+03	3.55422646.01	-3.6558693E+03	1.20102A7E+03
1 . 93000000 +01	4.2291006E+03	3.6402404F+01	-3.6712933F+03	1.109#234F+03
1.9400000F+01	4.24M6125E+03	3.68372976+01	-3.6788521E+63	1.1992235F+03
1.9600C00F+01	4.2875958E+03	3.77167276+01	-3.6936636F+03	1.19862565+03
1 - 9700000E +01	4.3070671E+03	3.8161306F+01	-3.7009162F+03	1-19743515+03
1.980CCOOF+G1	4.3265250F+03 4.3459694E+03	3.8609136F+01	-3.7080672F+03	1.19674266.03

TABLE 7. BEGINNING AND END OF OUTPUT FROM SAMPLE INPUT FOR SHELTRAJ (A) FORCES

PARAMETER ESTIMATION FOR ANALYSIS OF TRAJECTORY AND ROLL DATA FROM RADAR AND YAMSONDE MEASUREMENTS MADE DURING THE FLIGHT OF A SHELL A TEST EXERCISE FOR THE ANALYSIS OF RADAR DATA - NR3634 DRAG CURVE

VEHICLE PHYSICAL CONSTANTS
MASS 14.9688KG MOMENT OF INERTIA IN BOLL 0.023260KG M2
REFERENCE AREA 0.COR659M2 REFERENCE LENGTH 0.1050M

FARTH MODEL - ANGULAR VELOCITY LATITUDE FIRING LINE GRAVITATION HEIGHT ANDVE RADIUS OF

(RAD/SEC) (DEG) (DEG) (M/S/S) SEA LEVEL(M) THE FARTH(M)

0.72722000-04 35.000 315.000 9.80700 0.0 0.637335AD407

ORDER OF PARAMETERS
10 11 12 7 8 9 3 6 1 4 18 2 5 19 15 22 13 16 20 14 17 21 23 24 25 26 27

INITIAL TIME 0.0 (5)

SCALING OF RANGE AZIMUTH ALTITUDE POLL PATE

REJECTION LEVEL ON DATA 10.00

ACCURACY FACTOR FOR PARAMETER ERROR LEVELS 1.000
MAXIMUM INTEGRATION STEP 0.2000 NO. OF PARAMETERS VARIED 2 MAXIMUM NO. OF ITERATIONS 6
NO PLOTS PEQUESTED

	CDA0	CDBO	CDK	CDAI	CORI	CDL	XDO TO	YDOTO
PARAW.	-0.22900+00	-0.47340-01	0.97720+00	0.12630+00	0.46650-01	0.56330-01	F0+04P45.0	c.o
DELTA	0.50000-02	0.50000-02	0.10000-01	0.50000-02	0.50000-02	0.10000-02	0.10000+01	0.10000+01
	zoorn	*n	YO	20	CZALFAO	CZALFRO	CZALFAK	CZALFAI
PARAM.	-0.36370.03	0.0	0.0	0.0	-0.439AD+CO	-0.85000+00	0.96410+00	-0.73030+00
DELTA	0.10000+01	3.10000+01	0.10000+01	0.10000+01	0.10000-01	0.10000-01	0.10000-01	0.10000-01
	CZALFRI	CDAS	CDR2	CZALFAZ	CZALFR2	CZALFAL	CLPO	CLP1
PARAM.	0.13120-00	0.0	0.0	0.0	0.0	0.34410-01	-0.35590-01	0.15690-01
DELTA	0.10000-01	0.10000-02	6.10000-02	0.10000-01	0.10000-01	0.10000-02	0.10000-03	0.10000-03
	CLP2	CLPS	PC					
PAGAM.	-0.55770-02	E0-00M08.0	C.1390D+C4					
DELTA	0.50000-04	0.10000-04	0.10000-01					
SIGMA=	0.18207D+01 DEGR	EES OF FREEDO	H= 796					

COVARIANCE MATRIX (MATRIX IS SYMMETRIC)

1.250-08 -1.980-08 3.680-08

CHANGES TO THE FOLLOWING PARAMETERS ALL SMALL

	CDAG	CDAC	CDK	CDAI	CORI	CDL	*DO TO	YDOTO
PARAM.	-0.22760+00	-0.49540-01	0.97720+00	0.12630+00	0.46650-01	0.56330-01	0.28940+03	0.0
DELTA	0-11180-03	0.19180-03	0.10000-01	0.50000-02	0.50000-02	0.10000-02	0.10000+01	0.10000+01
	zonto	×0	¥0	zo	CZALFAO	CZALFRO	CZALFAK	CZALFAI
PARAM.	-0.36370+63	0.0	0.0	0.0	-0.93980+00	-0.85000+00	0.96410+00	-0.73030+00
DELTA	0.10000.01	0.10000+01	0.10000+01	0.10000+01	0.10000-01	0.10000-01	0.10000-01	0.10000-01
	CZALFRI	CDAZ	CDBS	CZALFAZ	CZALFBZ	CZALFAL	CLPO	CLPI
PARAY.	0.13120.00	0.0	0.0	0.0	0.0	0.34410-01	-0.35590-01	0.15690-01
DELTA	0.10000-01	0.10000-02	0.10000-02	0.10000-01	0.10000-01	0.10000-02	0.10000-03	0.10000-03
	CLPS	CLP3	99					
PAGAM.	-0.55770-02	C.89890-03	0.13900+04					
DEL TA	0.50000-04	0.10000-04	0.10000+01					

REJECTION LEVEL IN DATA 1.80

ACCURACY FACTOR FOR DADAMETER ERROR LEVELS 1.000 WAXIMUM INTEGRATION STEP 0.2000 NO. OF DADAMETERS VARIED 14 MAXIMUM NO. OF ITERATIONS 6 NO PLOTS REQUESTED

	CDAD	coen	COK	CDAI	COPI	COL	xnoto	YOUTO
DADAM.	-0.229PD+00	-0.44330-01	C.97690+00	0.12950+00	0.65340-01	0.57470-01	0.2889D+03	10-00100-01
DEL TA	0. 0000-02	0.50000-02	0.10000-01	6.50000-02	0.50000-02	0.10000-05	0.10000001	0.10000+01
	zonto	×o	*0	zn	CTALFAL	CZALFRO	CZALFAK	CZALEAT
PARA".	-0. 16400+03	0.13820+01	-0 . 74 94D-61	0.11080+01	-0.62320+00	-0.55000+00	0.96410+00	-C.73030.00
DELTA	0.10000+01	0.10000+01	C+10000+C1	0.10000+01	0.10000-01	0.10000-01	0.10000-01	C • 1 00 0r - 01
	CZALFRI	CDAZ	CDR2	CZALFAZ	CZALF#2	CZALFAL	CL PO	CLET
PARAM.	0.13120+00	0.0	C.0	6.0	0.0	0.34410-01	-C. 155 00-01	1.15600-01
DELTA	0.10000-01	0.10000-02	0.10000-62	0.10000-01	0.10000-01	0.10000-02	0.10000-03	0.10000-01

	CLDZ	CLPS	PO					
DAGAV.	-0.5770-02	G. MOMOD-03	0.13900+64					
DELTA	0. 00 Gn-C4	0.10000-04	0.10000+61					
SIGMA	C.4372674GC DEGR	FES OF FREEDO	H= 752					
	CDAD	Chan	cne	CDAI	coes	CDL	xmm	vooro
DADAW.	-0.2297D+CC	-0.44420-01	6.976BD+00	0.12900+00	0.45300-01	0.57350-01	0.28900463	5.51 gen-n2
DELTA	C. #9720-62	0.42090-02	6.70170-02	0.443-0-01	0-12710-01	0 . AR 390-62	0.43210+00	5.700AD-01

TABLE 7(A). (CONTINUED)

	20010	×O.	40	20	CZALFAD	CZALEBO	CZALFAK	CZALFAI
PAGA	-0.364CD+03	0.13260+01	-0.58160-C2	C-10650+C1	-6.91660+00	-C.F.C50+CG	0.46410+00	-C.73030+00
DELTA		0.20270.00	0.14920+00	0.24670+00	0.94510-01	0.15200-01	0.10020-01	1.10000-01
	CZALFRI	CDA2	CD82	CZALFAZ	CZALFE2	CZALFAL	cten	C1.6 1
PAGAS	. 0.13120.00	0.0	0.0	0.0	0.0	0. 34410-01	-0.15590-01	0.14600-01
DELT		0.10000-02	0.10000-02	C.1000D-01	0.10000-01	1000n-u2	6.16000-03	.10000-03
	CLPS	CLPS	PO					
DADA	-0.55770-02	E0-понов-03	C+139CD+64					
DEL T	0.50000-04	0.10000-04	0.1000D+01					
51 GM	A= 0.421390+00 DEG	DEES OF FREEDO	14= 74C					

COVADIANCE MATRIX (MATRIX IS SYMMETRIC)

7.650-05												
-3.070-05	1.800-05											
-5.490-05	1.670-05	4.570-05										
-1.720-64	1.380-04	2.730-04	1.860-03									
-9-119-05	5.900-05	4.350-05	4.020-04	1.990-04								
-5.24D-05	2.770-05	3.260-05	2.360-04	8.690-05	4.5AD-05							
2.9A0-03	-9.070-04	-2.230-03	-1 -600-02	-2.530-03	-1.520-03	1 . 740-01						
4.580-C6	-6.230-67	-4.140-05	-2 .AAD-05	-5.28D-07	-1.750-05	3.300-04	5.890-03					
-1.710-01	1-130-03	2.790-03	2.000-02	3-170-03	1.900-03	-2-170-01	-4-100-04	2.710-01				
-9-100-CA	2.630-04	A-950-04	5.350-03	7.180-04	4.300-04	-4.990-02	-1.350-04	8.630-02	3.830-02			
-5 - 360-67	-6-190-07	1.140-06	5.200-06	-2.950-06	-3.240-07	-1.140-04	-0.030-03	1.410-04	5.710-05	5.UNU-05		
1 180-17	-1-130-CA	-6-740-CA	-6-720-03	-4.200-04	-5.430-04	A.720-02	1.670-04	-1.000-01	-4.200-02	-6.920-05	5.660-02	
-1-170-06	1-570-06	-2.FAD-07	1.960-06	6.360-06	1.470-05	-0.H90-06	6.930-03	6.910-06	5.610-06	-1.670-02	-1.450-05	H.520-03
2.700-67	-1-690-07	5.830-08	-9-910-67	-1.630-06	-3.0FD-07	3.450-06	-7 -17D-G4	-4.770-05	A.030-08	7.500-04	2.540-06	-1.060-03
2.410-04	-3.630-01											
2.410-64												
				eure.								

CHANGES	TO	THE	FOLLOWING	PARAMETERS	ALL	SWALL

	CDAD	CDBC	CDK	CDAI	CDP1	CDL	KDOTO	YDOTO
DADAY.	-C.22960+00	-0.44440-01	C.97680+60	0.12890+00	C. F5470-01	0.57310-01	0.28960+03	C.52800-02
DELTA	C.8749D-C2	0.42470-02	0.67630-02	0.43080-01	0 - 14 1 00 - 01	0.67640-02	0.41750+00	0.76740-01
	20010	*O	¥0	20	CZALFAO	CZALERO	CZALFAK	CZALFAI
PARAM.	-0.36400+63	0.12720+01	-0.59920-02	0.10230+01	-0.91620+00	-0.8307D+00	0.96410+00	-0.73030+00
DELTA	0.52030.00	0.19560+06	0.14410+00	0.23800+60	10-00559+0	0-15540-01	0.10000-01	0.10000-01
	CZALFOI	CDA2	CDR2	CZALFA2	CZALFR2	CZALFAL	CLOC	CLP1
DARAM.	0.13120+00	0.0	C.C	0.0	0.0	C.34410-G1	-0.35500-01	0.15690-01
DEL. TA	0.10000-61	0.10000-02	0.10000-02	0.10000-01	0.10000-01	0.10000-02	0.10000-03	0.10000-03
	CLPS	CLP3	PO					
PARAM.	-0.55770-02	C. AGAGD-03	0.13900+04					
DE: **	0.5000000	0-10000-04	C-100000+C1					

TABLE 7. BEGINNING AND END OF OUTPUT FROM SAMPLE INPUT FOR SHELTRAJ (B) ROLLING MOMENTS

PARAMETER ESTIMATION FOR ANALYSIS OF TRAJECTORY AND BOLL DATA FROM RADAR AND YAMSONDE MEASUREMENTS MADE DURING THE FLIGHT OF A SHELL

A DECK TO TEST THE ROLL FITTING CAPABILITIES OF THIS PROGRAM

VEHICLE PHYSICAL CONSTANTS
WASS 14.9688KG MOMENT OF INERTIA IN ROLL 0.023266KG M2
REFERENCE LENGTH 0.1050M

FARTH HODEL - ANGULAR VELOCITY LATITUDE FIRING LINE GRAVITATION HEIGHT AROVE RADIUS OF

(RAD/SEC) (DEG) (M/S/S) SEA LEVEL(M) THE FARTH(M)

G.72722000-04 35.000 315.000 9.80700 0.0 0.63733680+07

ORDER OF PARAMETERS 6 7 M 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 1 2 4 5 3

INITIAL TIME 0.0 (5)

SCALING OF RANGE AZIMUTH ALTITUDE ROLL BATE 0.0 1.00 0.0 0.0

REJECTION LEVEL ON DATA 16.00

ACCURACY FACTOR FOR PARAMETER FEROR LEVELS 1.000
MAXIMUM INTEGRATION STEP 0.2000 NO. OF PARAMETERS VARIED 1 MAXIMUM NO. OF ITERATIONS 20
NO PLOTS REQUESTED.

CLPR CLPR PD CLP2 CLP3 Xn Yn Zn
-0.36660-61 6.16060-01 0.13900+64 0.0 0.0 C.12700+61 0.0 0.16200+01
0.50000-62 0.10000-02 0.10000+01 0.50000-03 0.10000-63 0.10000+01 0.10000+61 0.10000+61 CLPI CDAO COAL COL CDK 0.97680+00 0.57310-01 -0.22960+00 0.10000+00 0.50000-02 0.20000-01 0.12890+00 0.10000-01 0.10000-03 DEL TA COM2 CZALFAK CZALFAL CZALFAO CZALFAI
C.C 0.99419+00 c.39419-01 -0.91629+00 -0.73039+00
0.10009-03 0.10009+00 0.20009-02 C.10009+00 0.50009-01 CORO CDAI CZALFAZ -C.44440-C1 0.45470-01 0.50000-02 0.6 CZALFRI CZALFRZ ARAM. -0.83070+00 0.13120+00 0.0
DF.TA 0.5000+01 0.1000+01 0.1000-03
SI MAE 0.789470-01 DEGREES OF FREEDOM: 76 PO CLPO CLPI CLP2 CLP3 0.0 0.50000-03 0.10000-03 Yn 0.1600D-01 C.13900+04 0.12700+01 0.10000+01 0.10000+01 -0.4 1490-01 0.21420-04 DELTA CDA1 0.12890+60 6.10000-01 | X0010 | Y0010 | Z0010 | 0-2 '900+03 | 0-6 | -6-36400+03 | 0-1 | 0000+01 | 0-10000+01 | C-10000+01 CNK 0.976HD+00 CDAP COL CDAD 0.976H0+00 0.5731D-01 -0.2296D+00 0.1000D+00 0.5000D-02 0.2000D-01 PARAM. CZALFAL CZALFAC CDB1 CZALFAK CZALFAI CZALFAP 0.65470-01 0.0 0.50000-02 0.10000-03 0.96410+00 0.34410-01 -C.91620+00 -6.73030+00 0.20000-02 0.10000+00 0.50000-01 -0.4.440-01 0.50000-02 0.10000-03

CZALFRI CZALFR?

COVARIANCE MATRIX (MATRIX IS SYMMETRIC)

4-200-10

CHANGES TO THE FULLDWING PARAMETERS ALL SMALL

	CLPO	CLPI	PO	CLPS	CLPS	×n	Yn	70
	-0.41610-01	0.16000-01	0.13900+04	0.0	0.0	0.12700+01	0.0	0.10200+01
DELTA	0.24900-04	0.16000-02	0.10000+01	0.50000-03	0.10000-03	0.10000+01	0.10000+01	0.10000+01
	xooto	Y00 TO	700 10	COK	CDL	CDAD	COAL	CDAP
PAGAW.	0.28900+03	0.0	-0.36400+03	0.97680+00	0.57310-61	-0.22960+00	0.1289D+00	0.0
DELTA	0.10000+01	0.10000+01	6.10000+01	6.10000+00	C.50000-02	0.20000-01	0.10000-01	0.10000-03
	cnen	CORI	CDR2	CZALFAK	CZALFAL	CZALFAC	CZALFAI	CZALFAZ
PARAM.	-0.444AD-01	0.45470-01	0.0	0.94410+00	0.74410-01	-0.01520+00	-0.7303P+00	0.0
DELTA	0.50000-02	0.50000-02	0.10000-03	0.10000+00	0.20000-02	0.10000+00	0.50000-01	0.10000-03
	CZALFPO	CZALFRI	CZALFRZ					
P4944.	-0.836 70+CO	0.13120+00	0.0					
DEL TA	0.50000-01	0.10000-01	U-100CD-03					

TABLE 7(B). (CONTINUED)

ROLLIESTING - AC

REJECTION LEVEL ON DATA 0.18

ACCURACY FACTOR FOR PARAMETER EPROR LEVELS 1.000
MAXIMUM INTEGRATION STEP 0.2000 NO. OF PARAMETERS VARIED 4 MAXIMUM NO. OF ITERATIONS 20 NO PLOTS REQUESTED

	CLPO	CLPI	00	CLP2	CLES	×n	YO	20
PARAM.	-0.31920-01	0.72770-02	0.13900+64	0.0	0.0	0.12700+61	C.0	0.10200+01
DELTA	0.50000-02	0.10000-02	0.10000+01	0.50000-03	0.10000-03	0.10000+01	0.10000+01	0.10000+01
	xnoto	40010	700.10	CDK	CDL	CDAD	CDAI	CDAZ
PARAM.	0.28900+03	0.0	-0.36400+63	0.97AHD+00	0.57310-01	-0.22960+00	0.12890+00	0.0
DELTA	0.10000+01	0.10000+61	C.10000+01	0.10000+00	C.50000-02	0.20000-01	C-10000-01	0.10000-03
	CDRO	cnes	CDBS	CZALFAK	CZALFAL	CZALFAO	CZALFAI	CZALFA
PARAM.	-0.4440-01	0 -65470-01	0.0	0.96410+00	0.34410-01	-0.41620+00	-0.73030+00	0.0
DELTA	0.50000-02	0.50000-02	0.10000-03	0.1000D+0C	0.20000-02	0.10000+00	C.50000-01	0.10000-0
	CZALFRO	CZALFRI	C7ALFR2					
PARAM.	-0.83070+C0	0.13120+00	0.0					
DELTA	0.50000-01	0.10000-01	0.10000-03					
SIGMA=	0.605720-02 DEGH	EES OF FREEDO	ME TAR					
	CLPO	CLP1	90	CLP2	CLP3	×n	YC	2n
PARAM.	-0.34420-01	0.12700-01	0.13900+04	-0.2867D-02	0.0	0.12700+01	0.0	0.10200+0
DELTA	0.16890-04	0.36840-04	0.30410-02	0.19650-04	0.10000-03	0.10000+01	0.10060+01	0.10000+0
	xnoto	YOUTO	20010	cnx	COL	CDAD	COAL	CUVS

PARAM.	0.28900+03	0.0	-0.36400+03	0.97680+00	0.57310-01	-0.22960+00	0.12890+00	0.0
DELTA	0.10000+01	0.10000+01	C.1000D+01	0.10000+00	0.50000-02	0.20000-01	0.10000-01	0.10000-03
	COPO	CDR1	CDAZ	CZALFAK	CZALFAL	CZALFAD	CZALFAI	CZALFA?
PARAM.	-0.4440-01	0.65470-01	0.0	0.96410+00	0.34410-01	-0.91620+00	-0.73030+00	0.0
DELTA	0.50000-02	0.50000-02	0.10000-03	0.10000+00	0.20000-02	0.10000+00	0.50000-01	0.10000-0
	CZALFRO	CZALFRI	CZALFR2					
PARAM.	-0.83070+00	0.13120+00	0.0					
DEL TA	0.50000-01	0.10000-01	0.10000-03					
SIGMA=	0.63CA10-02 DEGR	EES OF FREEDO	M= 796					

COVARIANCE MATRIX (MATRIX IS SYMMETRIC)

2.720-10 -5.870-10 1.270-09 -2.830-08 6.480-08 7.340-06 3.080-10 -6.710-10 -3.630-08 3.550-10

CHANGES TO THE FOLLOWING PARAMETERS ALL SMALL

	CLPO	CLP1	PO	CLP2	CLP3	*n	YO	20
PARAP.	-0.34360-01	C+1258D-01	0.13900+04	-0.28010-02	0.0	0.12700+01	0.0	0.10200+01
DELTA	0.16490-04	0.35670-04	C . 27100-02	0-18840-64	0.10000-03	0.10000+01	0-10000+01	0.10000+01
	XDO TO	YDOTO	20070	CDK	CDL	CDAN	CDAI	CDAZ
PARAM.	C.2890D+G3	0.0	-0.36400+63	0.97680+00	0.57310-01	-0.22960+00	0.12000+00	0.0
DELTA	0.10000+01	0.10000+01	0.10000+01	0.10000+00	0.50000-02	0.20000-01	0.10000-01	C+10000-C3
	CDAD	CDAI	CDR2	CZALFAK	CZALFAL	CZALFAO	CZALFAI	CZALFAZ
PARAM.	-0.4440-01	0.65470-01	0.0	0.96410+00	0.34410-61	-0.91620+00	-0.73030+00	0.0
DELTA	0.50000-02	0.50000-02	6-10000-03	0.10000+00	0.20000-02	0.10000+00	0.50000-01	0.10000-03
	CZALFRO	CZALFRI	CSALFRE					
PARAM.	-0.63070+00	0.13120+00	C.0					
DEL TA	0-50000-01	0-10000-01	0.10000-03					

TABLE 8. DESCRIPTION OF CARD INPUT TO YAWCAL

Card	Format	Variable	Description
1	18A4	TITLE (18)	A 72 character description of the job.
2	6F10.0	X(3)	Initial estimates of the three parameters describing the calibration curve, equation (22) $\tan \sigma_N = -[\sin \alpha/X(1)] (1 + X(2)^2 - 2X(2) \cos \alpha)^{-\frac{1}{2}}$ where $\alpha = 2(\tau/T + X(3))$ X(3) is in radians. The three parameters are defined by X(1) = $\tan \gamma_1$, X(2) = $\tan \gamma_2/\tan \gamma_1$, and X(3) = β , where γ_1 , γ_2 and β are shown in figure 4.
3	1615	NPTS	Number of measured points on calibration curve.

NOTE: The three cards are followed by NPTS records on unit 4, each in 2F10.0 format, and each containing simultaneous values of time ratio, τ/T , and complementary solar aspect angle, $\sigma_{\rm N}$, in degrees.

TABLE 9. DESCRIPTION OF CARD INPUT TO ASPECT

Card	Format	Variable	Description
1	18A4	TITLE (18)	A 72 character description of the current job.
2	6F10.0	HA(I,J)	The hours, minutes and seconds, J=1, 2 and 3, of the hour angle of the first point of Aries at 0 hours Universal Time for the date being considered and the following day, I = 1, 2.
3	6F10.0	RA(I,J)	The hours, minutes and seconds, $J=1$, 2 and 3, of the right ascension of the sun at 0 hours Universal Time for the day in question and the following day, $I=1$, 2.
4	6F10.0	DE(I,J)	The degrees, minutes and seconds, J=1, 2 and 3, of the declination of the sun at 0 hours Universal Time for the day in question and the following day, I=1,2.
5	18A4	DATES(5)	A 20 character description of the date for which the complementary solar aspect angle is estimated.
6	6F10.0	LAT(3), LONG(3)	Degrees, minutes and seconds for latitude and longitude of shell. Latitude is positive north and longitude is positive west.
7	1215	NTIMES	Number of local times (local South Australian time) for which results are required. The local times used are corrected to Universal or Greenwich Mean Time in the program by subtracting nine and a half hours.
8	6F10.0	TO,DT	The local times should begin at TO hours and increment regularly by DT hours.
9	6F10.0	BEAR (3)	The degrees, minutes and seconds of the line of fire relative to true north.
10	1215	NELEVN	The number of elevation angles for which results are required.
11	6F10.0	ELO, DEL	The elevation angles should begin with ELO degrees and increment regularly by DEL degrees.

TABLE 10. DESCRIPTION OF CARD INPUT TO YAWSONDE

Read	Format	Variable	De	escription				
1	20A4	TITLE (20)	An 80 character job or reproduced on the out					
2	1615	LENTER	A control variable which can be used to begin entering data at any one of the following point he input stream.					
			LENTER	READ				
			1	3				
			2	6				
			3	7				
			4	8				
			5	9				
			6	10				
			7	11				
			8	12				
			9	14				
			10	return				
3	1615	NCOS		a table which provides the sun in range axes as a ng the trajectory.				
4	5E16.7	TIME(I), COSL(I), COSM(I), COSN(I)	Entries in the table set per card.	for I=1, NCOS with one				
5	1615	NTRAJ, IFOUT, ISKIP	a dataset constructed SHELTRAJ, further det are given in Section every ISKIP th point	up to a total of NTRAJ s used are recorded on the				
6	8F10.0	XE (12)	Maximum changes in ea are used in testing	ach parameter value, which for convergence.				
7	8F10.0	REFS BODIAM PITCHI ROLLI	Reference length for	erodynamic coefficients. aerodynamic coefficients. shell in pitch and yaw shell in roll.				
8	8F10.0	X(12)	Initial estimates for meters P _i .	r the values of the para-				
9	1615	JORDER (12)		ers for internal use by the when determining values for ameters.				
10	8F10.0	то	Time at which integra	ation begins.				
11	8F10.0	REJECT ACCFAC		ta rejection level. 11 the XE. Can be used ment of the convergence				

TABLE 10 (CONTINUED)

Read	Format	Variable	Description
		НМАХ	Maximum value for integration step. This value is used unless time to next data point is smaller.
12	1615	NPARAM ITERN NPLOT	The first NPARAM parameters only are allowed to vary. Maximum number of iterations. Plot every NPLOT th point of the simulated measurement values. A maximum of 500 points can be plotted.
13	1615	LENTER LCASE IFOUT	A repeat of the options allowed in read 2. Principally to avoid inputting new experimental data if none is required. Non-zero if data for another run follows. Non-zero if a record of the experimental data points is required in the print out.
14	1615	NPTS ISKIP	Number of experimentally measured data points to be used in this run. Uses every ISKIP th point from the dataset containing the experimental measurements.
15	1615	IND NWD NPT IFOUT	Control variable, describing the nature of the meteorological data which is available. =1 none available. =2 wind table only, =3 pressure and temperature table only, =4 both wind table and pressure and temperature table. Number of points in wind table. Number of points in pressure and temperature table. NON-zero if meteorological data should be recorded on printed output.

TABLE 11. SAMPLE INPUT DECK FOR YAWSONDE

1 2												
0.		-0.	. 6905	34		0.0114	01		-0.	723210		
.0.			.690	. 74		0.0114	01		-0.	723210		
10	1					01	0.			.1	1.	0.
0.001	1.	001	0.0	21		01	0.	••		••		
1. 0.008569		105		2557		02326						
0.1	0.4	427431	0.		0.		3.	76	0		0.	0.
0.	-1	٠.	0.		.0.				9	12	6	
,	1	3	•	5		10	7	11	-	12		
1.	1.		0.0	1								
1	20	C										
9	1	1										
100	1											
PART II												
2	20	C										
10	1											
PART III												
3	20	0										
10	1											
PART IV												
:	20	c										
10	1											
PART V												
10	20	c										
PART VI	1											
A												
	50	C										
PART VI	. 1											
A A	'											
7	20	c										
10	1											
PART VI	11											
-	20	0										
10	1											
•												
10	26	c										
PART X	•											
A												
10	20											
10	1											
PART XI												
11	20	0										
PART XI	. '											
12	20	1										
10												

TABLE 12. SIMULATED EXPERIMENTAL DATA FOR YAWSONDE

(A) TRAJECTORY MEASUREMENTS

18.000000	196.94579	9.71028	-89.705223566.139161207.80000
18.100000	196.79242	9.79641	-88.676693575.070691207.17249
18.200000	196.64590	9.88202	-87.635533583.898771206.54720
18.300000	196.50600	9.96349	-86.582633592.622201205.92411
18.400000	196.37213	10.03762	-85.519623601.239851205.30319
18.500000	196.24341	10.10182	-84.448733609.750841204.68442
18.600000	196.11874	10.15421	-83.372633618.154511204.06778
18.700000	195.99688	10.19369	-82.294233626.450471203.45325
18.800000	195.87654	10.21999	-81.216543634.638661202.84079
18.900000	195.75645	10.23362	-80.142433642.719291202.23040
19.000000	195.63549	10.23578	-79.074563650.692851201.62198
19.100000	195.51265	10.22829	-78.015163658.560091201.01551
19.200000	195.38711	10.21342	-76.965943666.321951200.41097
19.300000	195.25824	10.19376	-75.928033673.979491199.80833
19.400000	195.12568	10.17204	-74.901963681.533891199.20757
19.500000	194.98932	10.15102	-73.887643688.986331198.60868
19.600000	194.84927	10 - 13328	-72.884413696.337941198.01163
19.700000	194.70586	10.12116	-71.891093703.589791197.41640
19.800000	194.55960	10.11659	-70.906083710.742781196.82298
19.900000	194.41113	10.12105	-69.927453717.797651196.23134
20.000000	194.26120	10.13549	-68.953063724.754931195.64148

TABLE 12. SIMULATED EXPERIMENTAL DATA FOR YAWSONDE

(B) YAWSONDE MEASUREMENTS

1.8000000E+01	-3.3041852E-01	1.8265000E+01	-3.5929316E-01
1.8005000E+01	-3.3044029E-01	1.8270000E+01	-3.5955638E-01
1.8010000E+01	-3.3063585E-01	1.8275000E+01	-3.6012715E-01
1.8015000E+01	-3.3114431E-01	1 •8280000E+01	-3.6097965E-01
1.8020000E+01	-3.3199186E-01	1.8285000E+01	-3.6198605E-01
1.8025000E+01	-3.3308270E-01	1 • 8290000E+01	-3.6296266E-01
1.803000E+01	-3.3423385E-01	1.8295000E+01	-3.6373594E-01
1.8035000E+01	-3.3524110E-01	1 .8300000E+01	-3.6420481E-01
1.8040000E+01	-3.3595251E-01	1.8305000E+01	-3.6437677E-01
1.8045000E+01	-3.3632292E-01	1.8310000E+01	-3.6436477E-01
1.8050C00E+01	-3.3642983E-01	1.8315000E+01	-3.6434621E-01
1.8055000E+01	-3.3644504E-01	1.8320000E+01	-3.6449900E-01
1.8060000E+01	-3.3657236E-01	1.8325000E+01	-3.6493775E-01
1.8065000E+01	-3.3697433E-01	1.8330000E+01	-3.6567298E-01
1.8070000E+01	-3.3771395E-01	1.8335000E+01	-3.6660771E-01
1.8075000E+01	-3.3873251E-01	1 . 8340000E+01	-3.6757249E-01
1.8080000E+01	-3.3987099E-01	1.8345000E+01	-3.6838643E-01
1.8085000E+01	-3.4092745E-01	1.8350000E+01	-3.6892209E-01
1.8090000E+01	-3.4172973E-01	1.8355000E+01	-3.6915110E-01
1.8095000E+01	-3.4219726E-01	1.8360000E+01	-3.6915405E-01
1.8100000E+01	-3.4236978E-01	1.8365000E+01	-3.6909107E-01
1.8105000E+01	-3.4239251E-01	1.8370000E+01	-3.6914402E-01
1.8110000E+01	-3.4246355E-01	1.8375000E+01	-3.6945122E-01
		1.8380000E+01	-3.7005806E-01
1.8115000E+01	-3.4276237E-01		
1.8120000E+01	-3.4338553E-01	1.8385000E+01	-3.7090111E-01
1.8125000E+01	-3.4431235E-01	1.8390000E+01	-3.7183115E-01
1.8130000E+01	-3.4541267E-01	1.8395000E+01	-3.7266689E-01
1.8135000E+01	-3.4649392E-01	1.8400000E+01	-3.7326010E-01
1.8140000E+01	-3.4737044E-01	1.8405000E+01	-3.7354870E-01
1.8145000E+01	-3.4793015E-01	1.8410000E+01	-3.7357878E-01
1.8150000E+01	-3.4817470E-01	1.8415000E+01	-3.7348765E-01
1.8155000E+01	-3.4821840E-01	1.8420000E+01	-3.7345417E-01
1.8160000E+01	-3.4824668E-01	1.8425000E+01	-3.7363445E-01
1.8165000E+01	-3.4844911E-01	1 • 8430000E +01	-3.7410604E-01
1.8170000E+01	-3.4895135E-01	1.8435000E+01	-3.7484046E-01
1.8175000E+01	-3.4977035E-01	1.8440000E+01	-3.7571377E-01
1.8180000E+01	-3.5080864E-01	1.8445000E+01	-3.7655119E-01
1.8185000E+01	-3.5188960E-01	1 • 8450000E+01	-3.7718995E-01
1.8190000E+01	-3.5282113E-01	1.8455000E+01	-3.7753757E-01
1.8195000E+01	-3.5346462E-01	1.8460000E+01	-3.7760493E-01
1.820000E+01	-3.5378470E-01	1.8465000E+01	-3.7750192E-01
1.8205000E+01	-3.5386154E-01	1.8470000E+01	-3.7739764E-01
1.8210000E+01	-3.5386160E-01	1.8475000E+01	-3.7745953E-01
1.8215000E+01	-3.5397740E-01	1.8480000E+01	-3.7779339E-01
1.8220000E+01	-3.5435834E-01	1.8485000E+01	-3.7840581E-01
1 .8225000E+01	-3.5505729E-01	1.8490000E+01	-3.7920209E-01
1.8230000E+01	-3.5601197E-01	1.8495000F+C1	-3.8002052F-01
1.8235000E+01	-3.5706769E-01		
1.8240000E+01	-3.5803301E-01		
1.8245000E+01	-3.5874866E-01		
1.8250000E+01	-3.5914460E-01		
1.8255000E+01	-3.5926495E-01		
1.8260000E+01	-3.5925168E-01		
	31312310112 01		

TABLE 13. BEGINNING AND END OF OUTPUT FROM SAMPLE INPUT TO YAWSONDE

PARAMETER ESTIMATION FOR ANALYSIS OF YAWSONDE DATA FROM RADAR AND YAWSONDE MEASUREMENTS MADE DURING THE FLIGHT OF A SHELL TEST DECK FOR YAWSONDE DATA ANALYSIS PROGRAMME

```
DIRECTION COSINES FOR THE SUN IN RANGE AXES AS A FUNCTION OF TIME ALONG THE TRAJECTORY
TIME(S) L H N
0.0 -0.690634 0.011401 -0.723210
40.00 -0.690634 0.011401 -0.723210
```

TABULATED TRAJECTORY DATA

```
TIME XDDI YDDI ZDDI ALT ROLL (SEC) (METRES/SECOND) (M) (RAD/SEC) (METRES/SECOND) (M) (RAD/SEC) (
```

VEHICLE PHYSICAL CONSTANTS

REFERENCE AREA= 0.008569(M**2) PITCH INERTIA= 0.225570(KG M**2)

PODY DIAMETER= 0.1050(M)
ROLL INERTIA= 0.0232600(KG M**2)

ORDER OF PARAMETERS
2 1 3 4 5 8 10 7 11 9 12 6

STARTING TIME= 18.000(5)

INITIAL MESECTION LEVEL ON DATA 400
ACCUBACY FACTOR FOR DARAMETER FROM LEVELS 1.000
MAXIMUM INTEGRATION STEP 0.0100
NUMBER OF DARAMETERS VARIED 1
MAXIMUM NUMBER OF ITERATIONS 20

NO PLOTS REQUESTED

TIME COMPLEMENTARY SOLAR (SEC) ASPECT ANGLE(DEG) 18.0000 -0.33041852 18.0050 -C.33044029 -0.33063585 -0.33114431 -0.33199186 18.0100 18.0100 18.0150 18.0200 18.0250 18.0350 18.0350 18.0400 18.0450 18.0506 18.0550 18.0650 18.0650 -0.33632292 -0.33642983 -0.33644504 -0.33657236 -0.33697433 -0.33771395 -0.33873251 -0.33877099 18.0700 18.0750 18.0800 18.0850 -0.33987099 -0.34092745 -0.34172973 -0.34219726 -0.34236978 -0.34236951 -0.34276235 -0.34276237 -0.34338553 -0.34431235 18-1150 18-1250 18-1250 18-1250 18-1350 18-1350 18-1450 18-1500 18-1600 18-1600 18-1750 18-1750 18-1750 18-1750 18-1800 18-1800 -0.34431235 -0.34549392 -0.34737044 -0.34793015 -0.34817470 -0.34821846 -0.34824668 -0.34097035 -0.33097035 -0.35090464 -0.355184060 -0.3552113 -0.3538660 -0.35386160 -0.35386160 -0.35386160 -0.353876360 -0.35637670 -0.35637670 -0.35637676 -0.35637676 -0.35637676 -0.35637676 -0.35637676 18.1950 18.2000 18.20%
18.21%
18.21%
18.22%
18.23%
18.23%
18.24%
18.25%
18.25%
18.26%
18.25%
18.25%
18.25%
18.25%
18.26%
18.27%
18.27%
18.27% -0.35050316 -0.35055638 -0.16012715 -0.16097065 -0.16191605 -0.16296766

TABLE 13. (CONTINUED)

FLTA	-0.14000+02 C.10000+61 18010D-03 DEGRE	0.0	0.3 C.10000+61	0.0				
	CMOO	CM5	CNP3	CMUS				
SEL TA	0.4274D+GC 0.100CD-02	0.10000-02	0.10000-01	0.0 0.10000-01	0.37600+01	0.10000-01	0.0	0.0
	THE TAD	PS10	00	RU	CM1	CHMACH	CNPI	CM3
18.4950	-0.380026	52						
18.4900	-0.379202							
18.4850								
18.4900	-0.377793	39						
18.4750	-0.377459	53						
18.4700	-0.377397	64						
18.4650	-0.377501	92						
18.4600	-0.377604	93						
18.4550	-0.377537	57						
18.4500	-0.377189	95						
18.4450								
18.4400								
18.4350								
18.4300								
18.4250								
18.4200								
18.4150								
18.4100								
18.4050								
18.4000								
18.3950								
18.3900								
18.3850								
18.3750								
18.3750								
18.3700								
18.3600								
18.3550								
18.3500								
18.3450								
18.3400								
18.3350								
18.3300								
18.3250								
14.3200								
18.3150	-0.364346	21						
18.3100	-0.364364	77						
18.3050	-0.364376	77						
18.3000	-0.364204	AI						
18.2950	-0.363735	94						

COVARIANCE MATRIX (MATRIX IS SYMMETRIC)

4.550-16

CHANGES TO THE FOLLOWING PARAMETERS ALL SMALL

	THETAD	PS10	90	RO	CWI	CMMACH	CNP1	CM3
DELTA	0.42710+00	0.10000-00	0.0	0.0 0.1000D-01	0.3760D+01 0.1000D+00	0.0 0.1000D-01	0.0	0.0
	CM06	CM5	CNP3	CMUS				
DEL TA	0.10000+02	0.0 0.1000D+01	0.10000+01	0.0				

PART XI.

INITIAL REJECTION LEVEL ON DATA 0.00
ACCURACY FACTOR FOR PARAMETER ERROR LEVELS 1.000
MAXIMUM INTEGRATION STEP 0.0100
MINNER OF PARAMETERS VARIED 12
MAXIMUM NUMBER OF ITERATIONS 20

PLOTS REQUESTED EVERY 1 POINTS

	THE TAO	PS 10	00	RO	CMI	CMMACH	CNPI	CM3
PARAM.	0.42740+00	0.10010+00	0.45300-05	-0.10670-03	0.37190+01	0.13450+00	0-16840-01	-0.49370+01
DELTA	0.10000-02	0.10000-02	0.10000-01	0.10000-01	0.10000+00	0.10000-01	0.10000+00	0.10000+00
	CPOC	CMS	CNP3	CMUS				
PARAM.	-0.14340+02	0.17270+04	-6.13230+01	0.0				
DELTA	0.10000+01	0.10000+01	C-10000+01	0.10000+01				
SIGMA	0.786100-07 DEGR	ES OF FREEDO	M= 99					
	THETAN	PS 10	90	RO	CPI	CHMACH	CNP1	C#3
PARAM.	0.42740+00	0.10000+00	0.42940-05	-0.69760-04	0.35900+01	0.34110+00	0.70430-03	-0.77540+01
DELTA	0.44780-05	0.58120-04	0.43560-05	0.50780-04	0.19410+00	0.30330+00	0-19400-01	0.43960+01
	C#00	CMS	CNP3	CM02				
PARAM.	-0.14160+02	0.20460+04	0.47210+01	-0.1264D+03				
DELTA	0.20700+00	0.78110+03	0.72480+01	0.14460+03				
SIGMA	G.786100-07 DEGRE	ES OF FREEDO	W= 99					

4.79200-08
3.21440-08
3.21440-08
4.63910-09
-2.09090-08
-9.08140-09
-1.31270-07
-1.31270-07
-1.31270-07
-1.31270-07
-1.31270-07
-1.31270-07
-1.3290-08
-1.42710-08
-1.42710-08
-1.42710-08
-1.42710-08
-1.42710-08
-1.42710-08
-1.42720-07
-1.51280-07
-1.51280-07
-1.131280-07
-1.131280-07
-1.131280-07
-1.3390-08
-1.43390-08
-1.43390-08

TABLE 13. (CONTINUED)

COVARIANCE MATRIX (MATRIX IS SYMMETRIC)

PARAM.	-0.1416D+	02 0.20	460+04	0.47300+01 0.72710+01	-0.1265D+						
	CMOO		CM5	CNPS	CMUS						
DELTA	0.44570-	05 0.57	BBD-04 (.43520-05	0.50650-	0.193	20+00 0	.30200+00	0.19390-01	0.43970	+01
ARAM.	0.42740+	00 0.100	000+00	.4307D~05	-0.69900-	0.359	10+01 0	.34030+00	0.72200-03		
	THETA	0	PSIO	. 00	RO			CMMACH	CNPI	CM	3
CHANGES TO	THE FOLLO	HING PARA	METERS ALL	SMALL							
-6.060-04	7.870-03	3.760-05	-6.120-03	2.130.01	-3.410+01	2.670+00	•••	2 -2.4.01	-4.5411404	1.010.02	2.1
	-4.100-04			-1.060.00							2.100+
	-1.960-05					-6.85D+0C			3-100+03	5.290+01	
	-1.0AD-05	6.480-09		-3.240-02		-3.640-03					
-1.440-05	1.850-04		-1 -1 30-04		-4.960-01	6.340-02					
-A.61D-0A	1.120-06		-8.960-07		-5.060-03						
1.200-06	-1.560-05			-5.830-02							
-7.530-07	9.810-06	2.100-07	-9.580-06	3.730-02							
2.120-10	-2.760-09	-5.730-11	2.570-09								
-5.380-12	6.910-11	1.890-11									
-2.580-10	3.350-09										

TIME (S)	COMPLEMENTARY SOLA			
	SOLAR ASPECT ANGLE			
18.005	-(.3304464	6.6066D-0A	16.300	-0.3642049
18.010	-0.3306350	4.91690-0A	18.305	-0.364376F
18.015	-0.3311443	3.46230-06	18.310	-0.364364R
18.020	-6.3310919	8.09630-09	18.315	-0.3643462
18.025	-C.3330P27	-1.10510-08	18.320	-0.3644989
18.030	-C.334233A	-2.48P3D-08	16.325	-0.3656729
18.035	-0.3352411	-4.15680-GR	16.335	-0.3666076
14.040	-6.3363229	-5.4128D-08	18.340	-6.3675724
18.050	-C.336429A	-6.35060-08	18.345	-0.3683863
18.055	-6.3364450	-8.9345D-08	16.350	-G.3689220
18.060	-0.3365723	-9.09660-08	16.355	-0.3691511
18.065	-6.1369742	-A. 38160-0P	18.360	-0.3691541
18.070	-6.3377139	-4 . A2450-0A	16.365	-0.3690911
18.075	-6.3387325	-7.01790-09	18.370	-0.3691441
18.CA0	-C .3398710	3.47560-0H	16.375	-0.3694514
18.085	-6.3409275	7.45920-OR	18.380	-0.37005R2
18.090	-0.341729A	9.765AD-0H	18.385	-0.3709013
18.095	-0.3421974	1.07050-07	18.390	-0.3718313
18.100	-6.3423699	9.16180-08	18.395	-0.3726670
18.105	-6.3423926	A. AAAAD-OR	18.400	-0.3732602
18.110	-0.3424636	6.43620-0R	18.405	-C.3735487
18.115	-0.3427624	4.61500-08	16.410	-C.3735788
18.120	-0.3433856	3.03430-0P	18.415	-G.3734876
18.125	-0.3443124	5.70590-10	18.420	-0.3734541
18.130	-6.3454126	-2.251 AD-OA	18.425	-0.3736343
18 - 135	-0.3464939	-3.83590-0A	18.430	-6.3741059
18.140	-6.3473704	-6.1747D-0H	16.435	-0.374A403
18.145	-6.3479301	-A.82580-08	17.440	-0.3757137
18.150	-G.3481746	-7.0701D-OR	17.445	-6.3765511
18-155	-0.34R21R3	-5.97300-0A	18.450	-0.3771A99
18.160	-C.34P2466	-4.74560-0A	18.455	-0.3775376 -0.3776049
18-145	-0.3484491 -C.3489514	A.4553D-09	18.460	-0.3775019
18-170	-0.3497704	4.59640-06	18.470	-6.3773977
18.180	-C.3508087	6.83210-08	16.475	-(.3774596
10.105	-C.3518897	8.92610-08	15.480	-6.3777934
18.190	-0.3528212	8.2788D-08	16.485	-6.3784059
18.195	-0.3534647	7.57850-08	15.490	-0.3792021
18.200	-C.3537848	6-12530-08	16.495	-0.3P00205
18.205	-0.3538616	5.41910-0A		
14.210	-0.3536616	3.37160-08		
18.215	-0.3539774	7.47030-09		
18.220	-0.35435R3	-2.59540-08		
18.225	-0.3550572	-6.6804D-08		
18.230	-0.3560119	-9.31 72n-08		
18.235	-0.3570676	-1.22500-07		
18.240	-0.3580320	-1.23510-07		
18.245	-0.35A74A5	-1-1814D-07 -9-4587D-08		
18.250	-0.3591445	-5.90120-08		
18.255	-0.3592517	-5.90120-0F		
10.200	-0.3592932	1.36210-08		
18.270	-0.3595564	3-96770-06		
18.275	-0.3401272	7.44 850-08		
10.200	-6.3609797	A-50770-06		
10.200	-0.3619861	9.27890-08		
18.290	-0.3629627	A-15930-0F		
18.795	-0.3637360	A-10310-08		

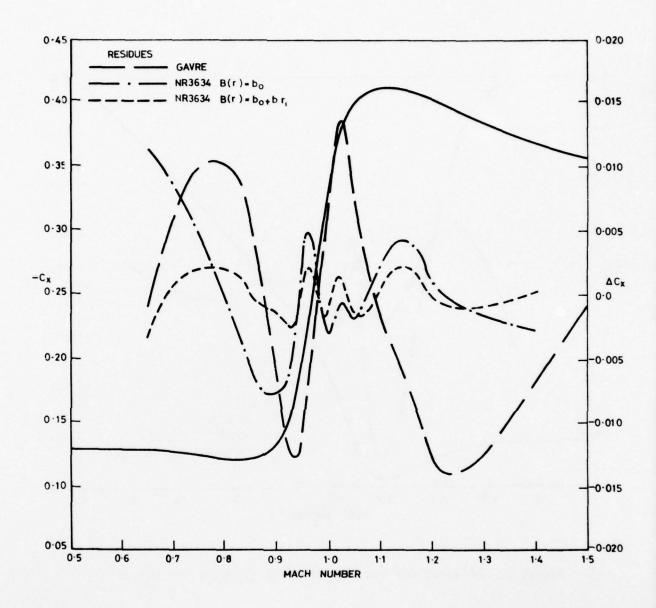


Figure 1. Residues for fitted axial force curves

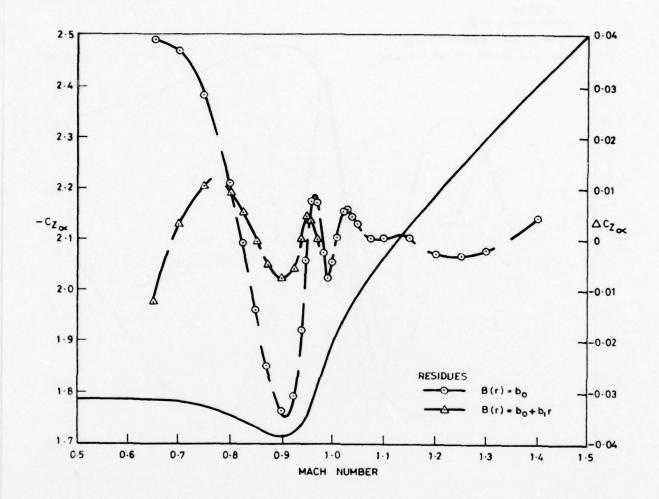


Figure 2. Residues for fitted normal force derivative curves

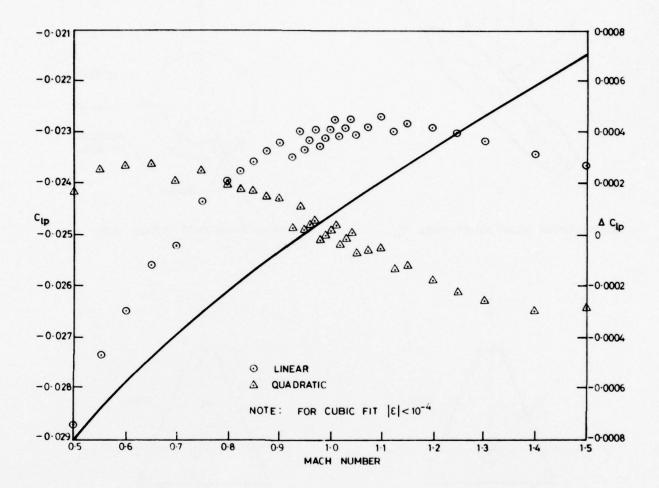
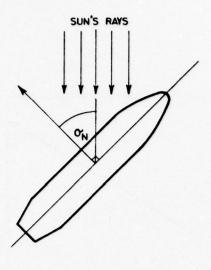
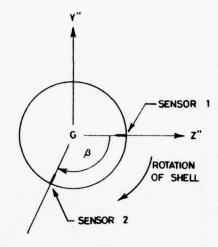


Figure 3. Residues for fitted roll damping derivative curves

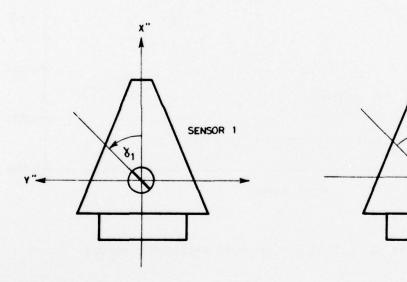


(a) COMPLEMENTARY SOLAR ASPECT ANGLE O'N



SENSOR 2

(b) ANGLE OF ROTATION BETWEEN SLITS



(c) ORIENTATION OF SLITS RELATIVE TO THE LONGITUDINAL AXIS OF THE SHELL

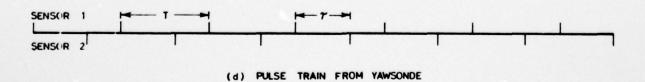


Figure 4. Schematic representation of a yawsonde

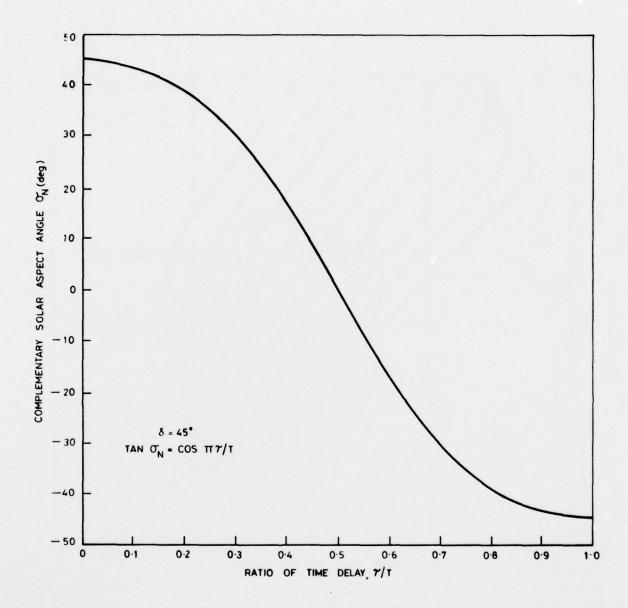


Figure 5. Typical yawsonde calibration curve

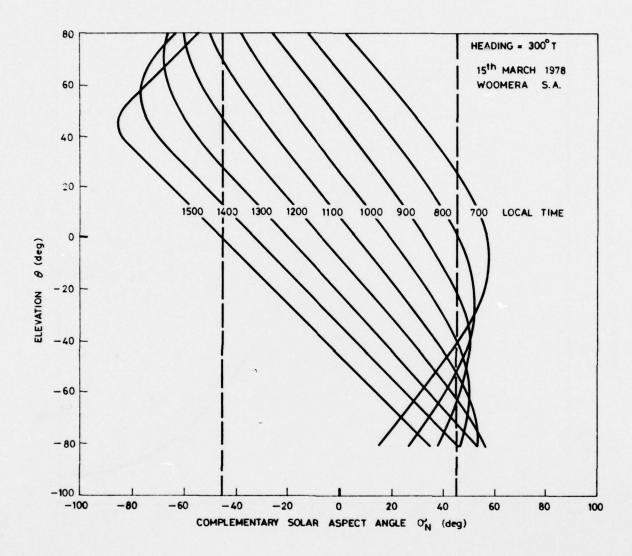
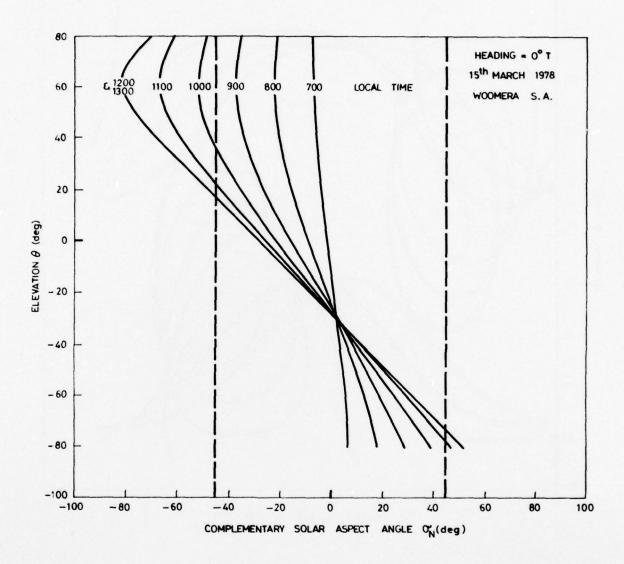


Figure 6. Variation of complementary solar aspect angle with shell elevation

(a) heading 300 degrees T



(b) heading due north

Figure 6. Variation of complementary solar aspect angle with shell elevation

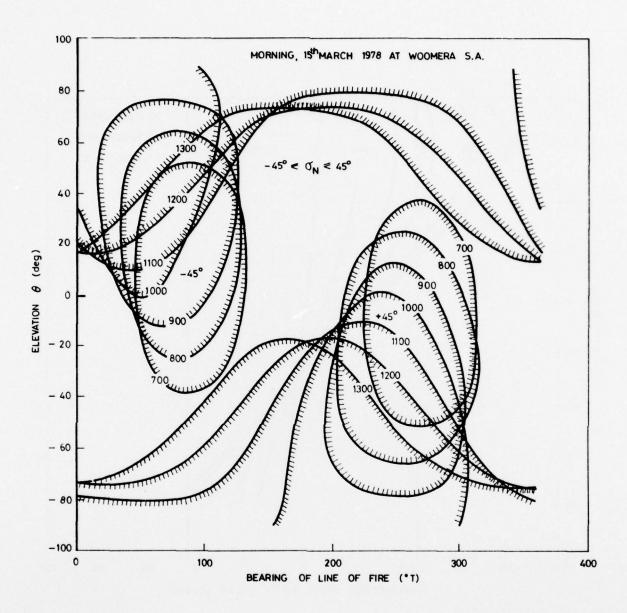
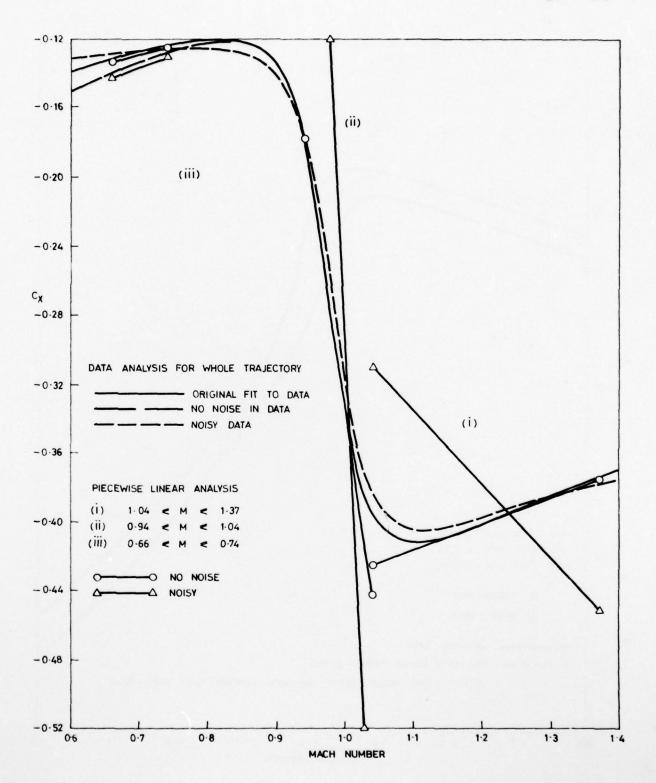
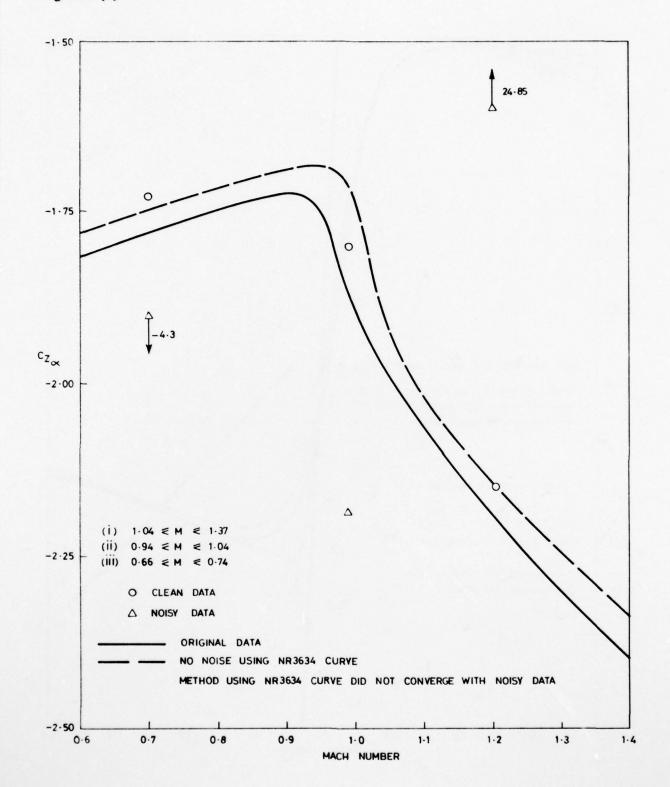


Figure 7. Conditions for detecting the sun



(a) axial force

Figure 8. Comparison of methods for estimating aerodynamic force coefficients



(b) normal force derivative

Figure 8. Comparison of methods for estimating aerodynamic force coefficients

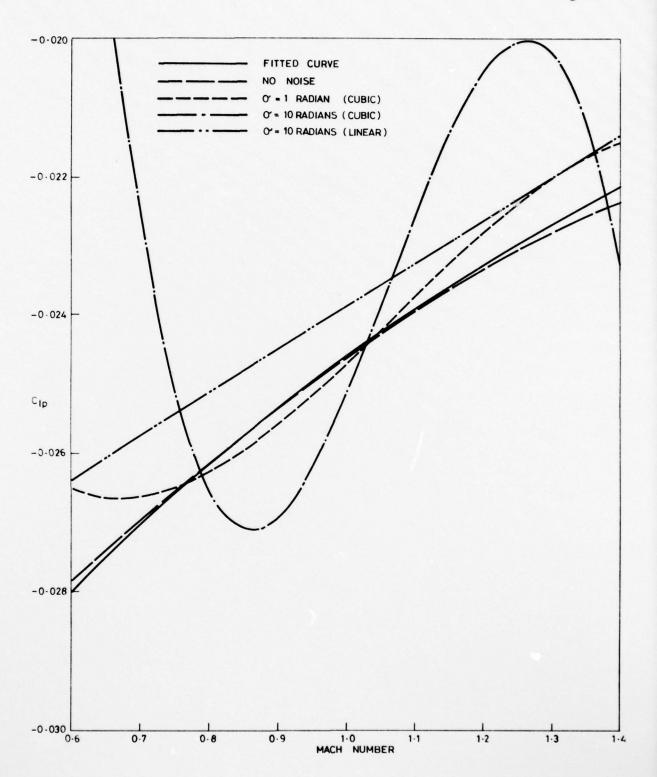


Figure 9. Effects of noise on estimation of roll damping moments

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THE ANALYSIS OF TRAJECTORY AND SOLAR ASPECT ANGLE RECORDS OF SH--ETC(U)

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